

# **INTRODUCTION TO OCEAN** **MODELING**

[Joseph K. Ansong](#)

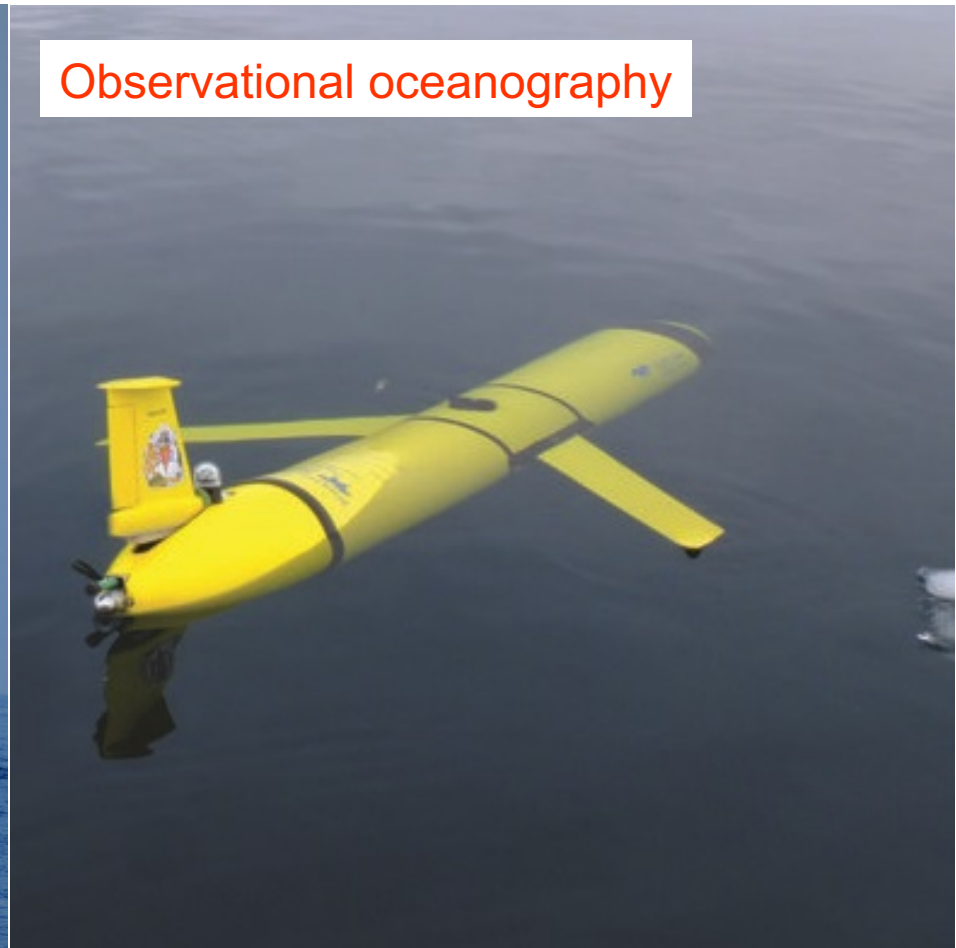
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(University of Ghana)

*COESSING-2018*

# OUTLINE

- INTRODUCTION
- MOTIVATION
- EQUATIONS OF MOTION
- EXAMPLES
- CHALLENGES

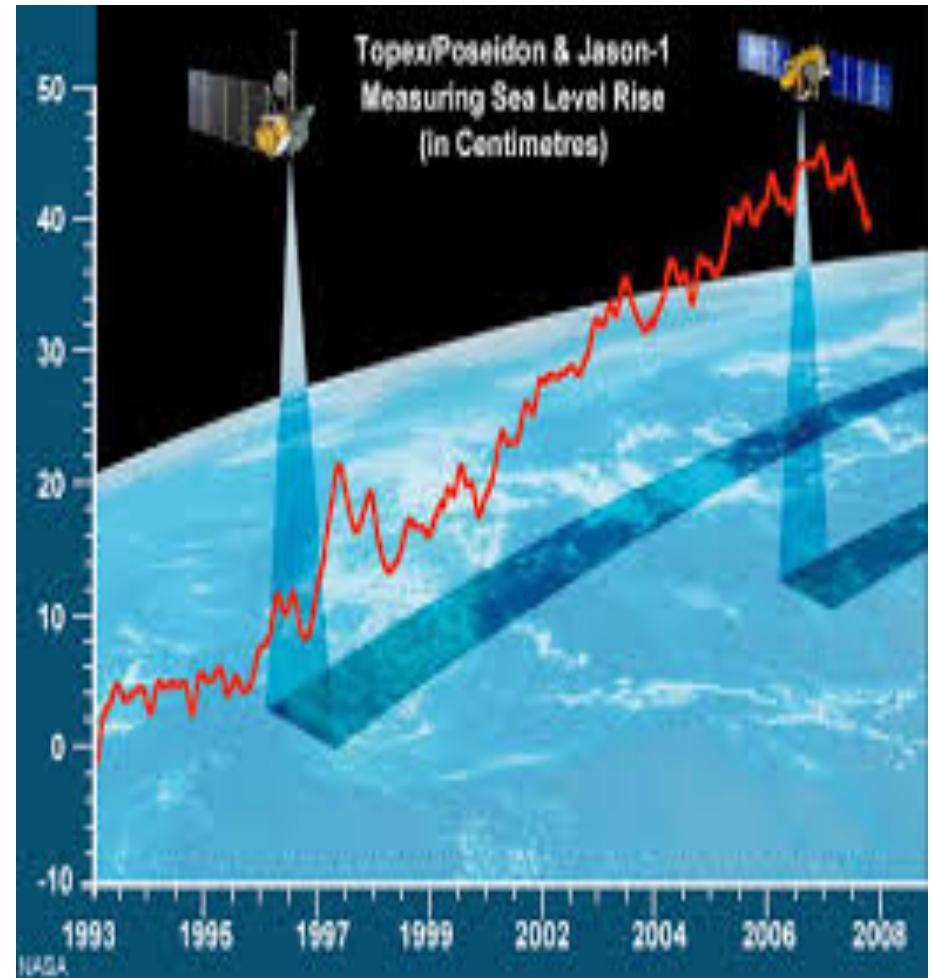
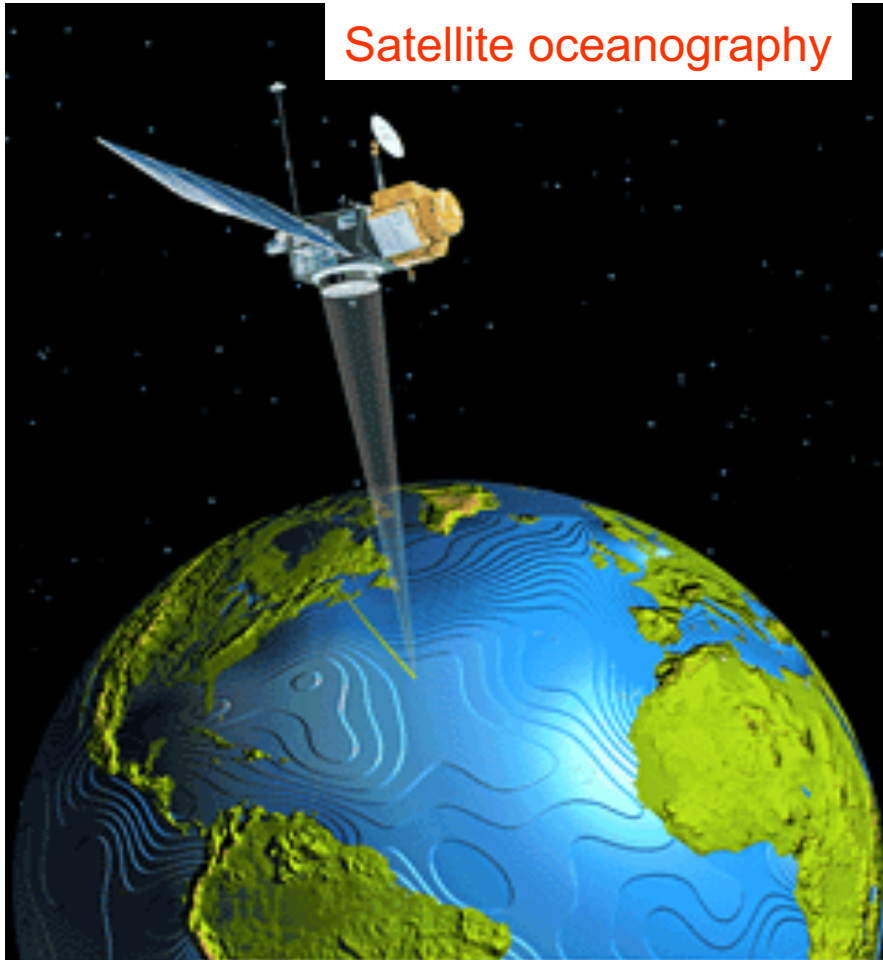
# Introduction: Approaches to oceanic studies



**Emily/Stephan et al.**

# Introduction: Approaches to oceanic studies

Satellite oceanography



Ebenezer et al.

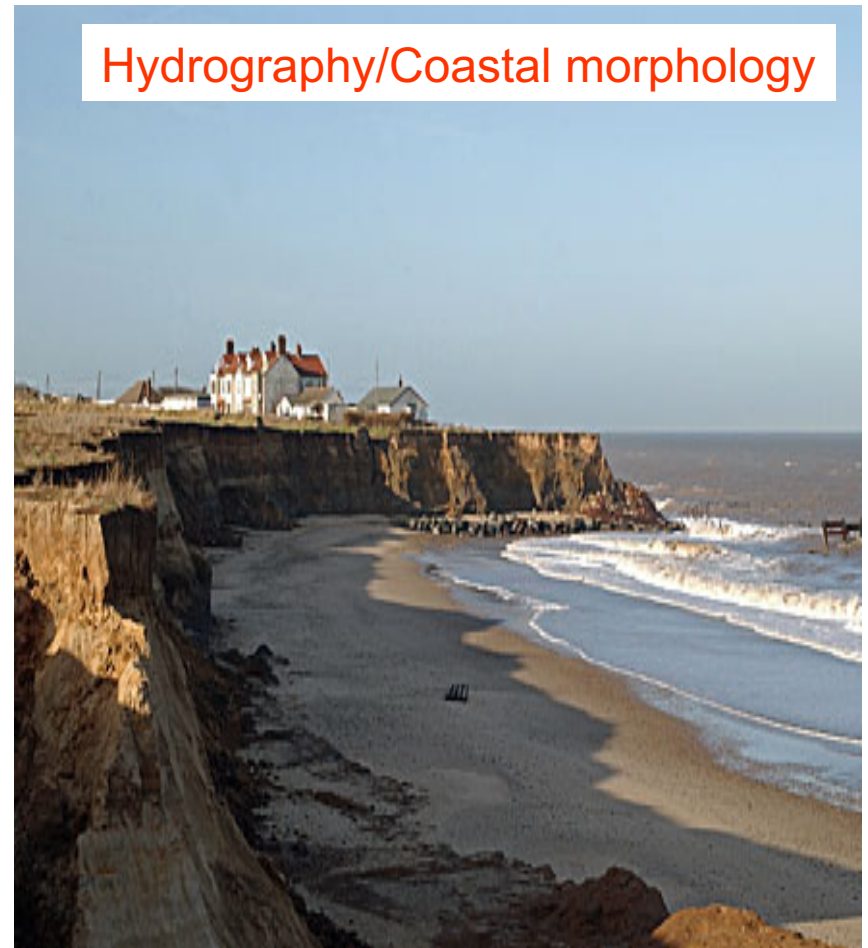
# Introduction: Approaches to oceanic studies

Chemical oceanography



Winn et al.

Hydrography/Coastal morphology

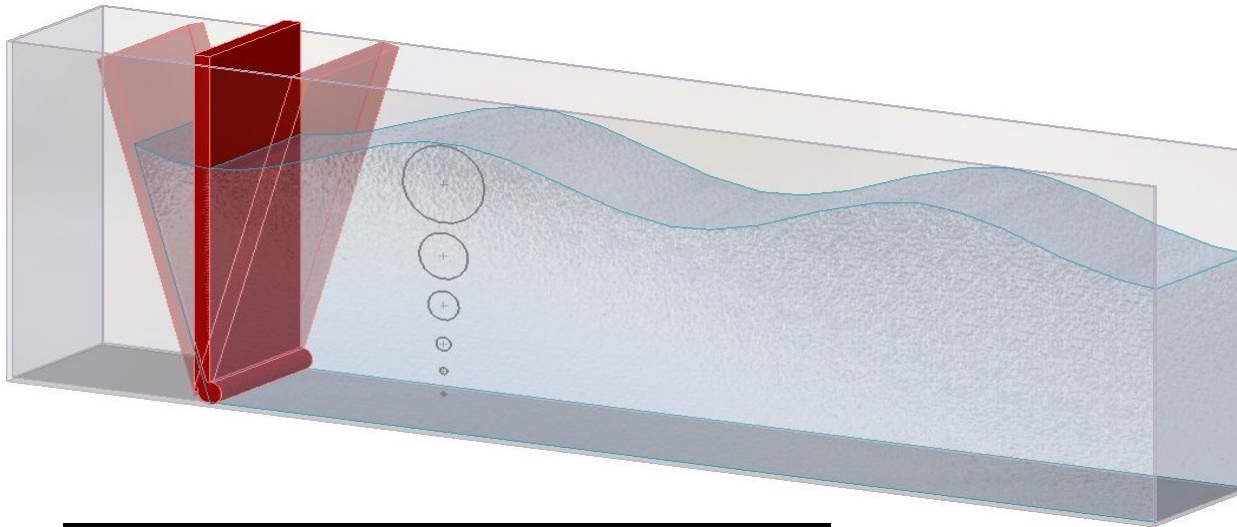


Stephan/Kwasi/Edem et al.

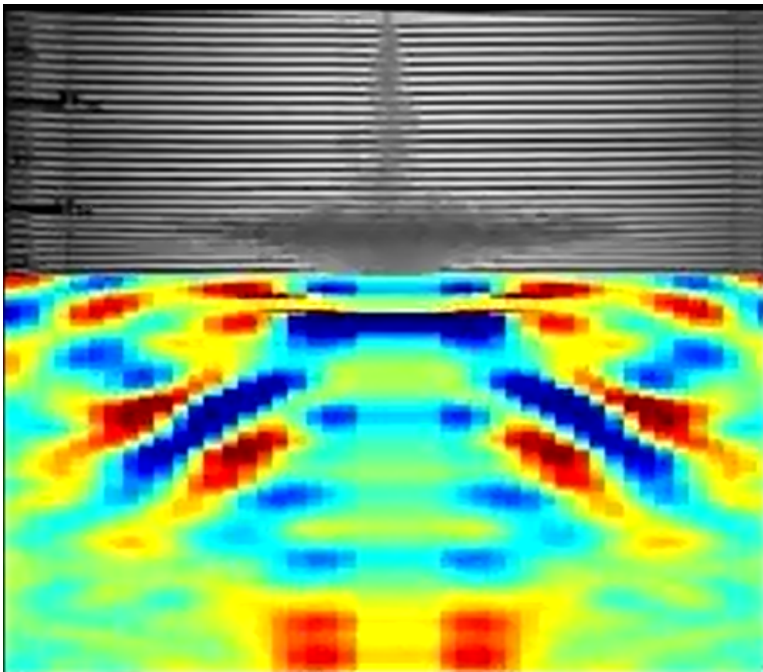


Angela et al.

# Introduction: Approaches to oceanic studies

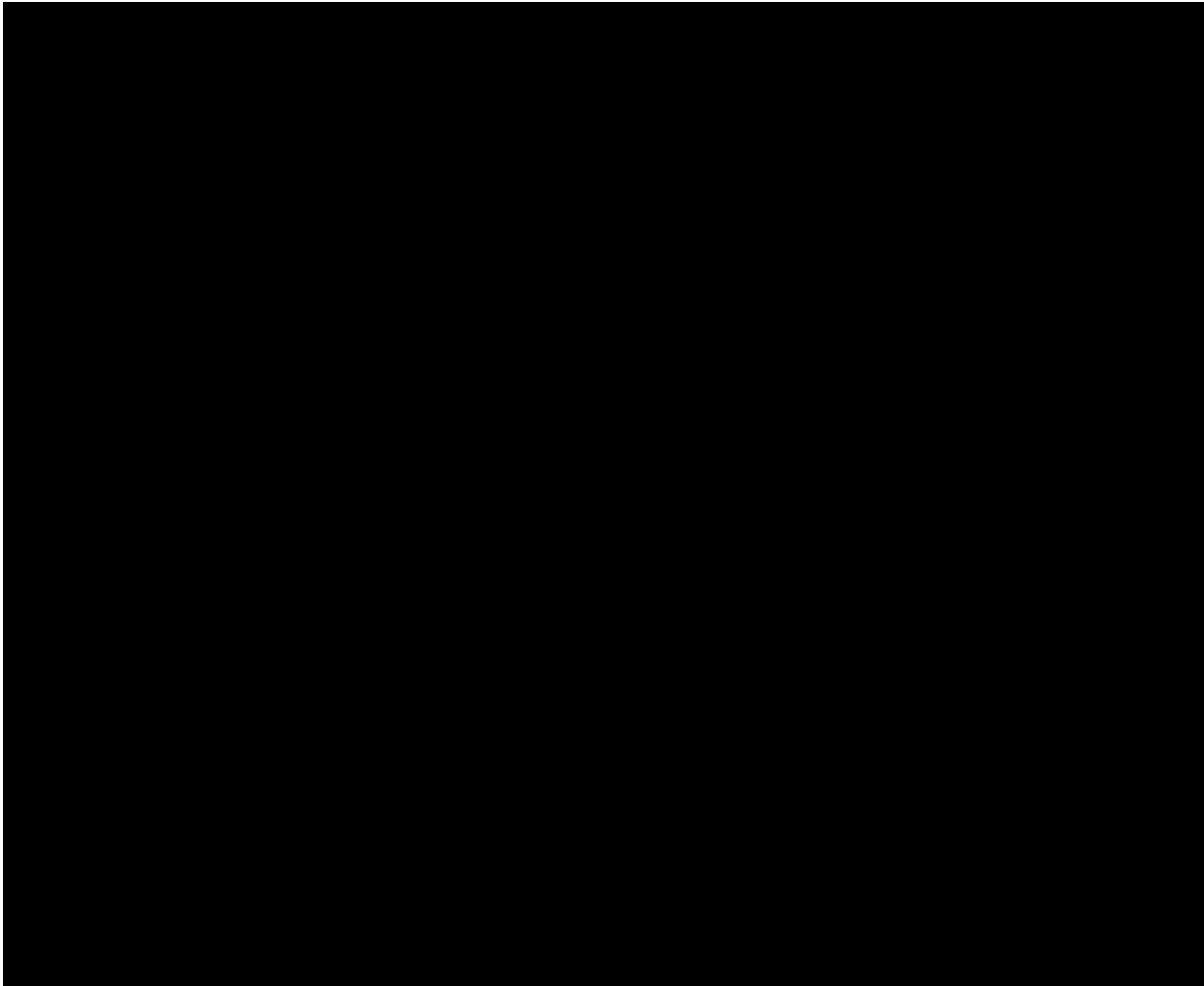


**Laboratory tank  
Experiments-  
Emily/Stephan**



**Ansong & Sutherland,  
2010, JFM, vol 648**

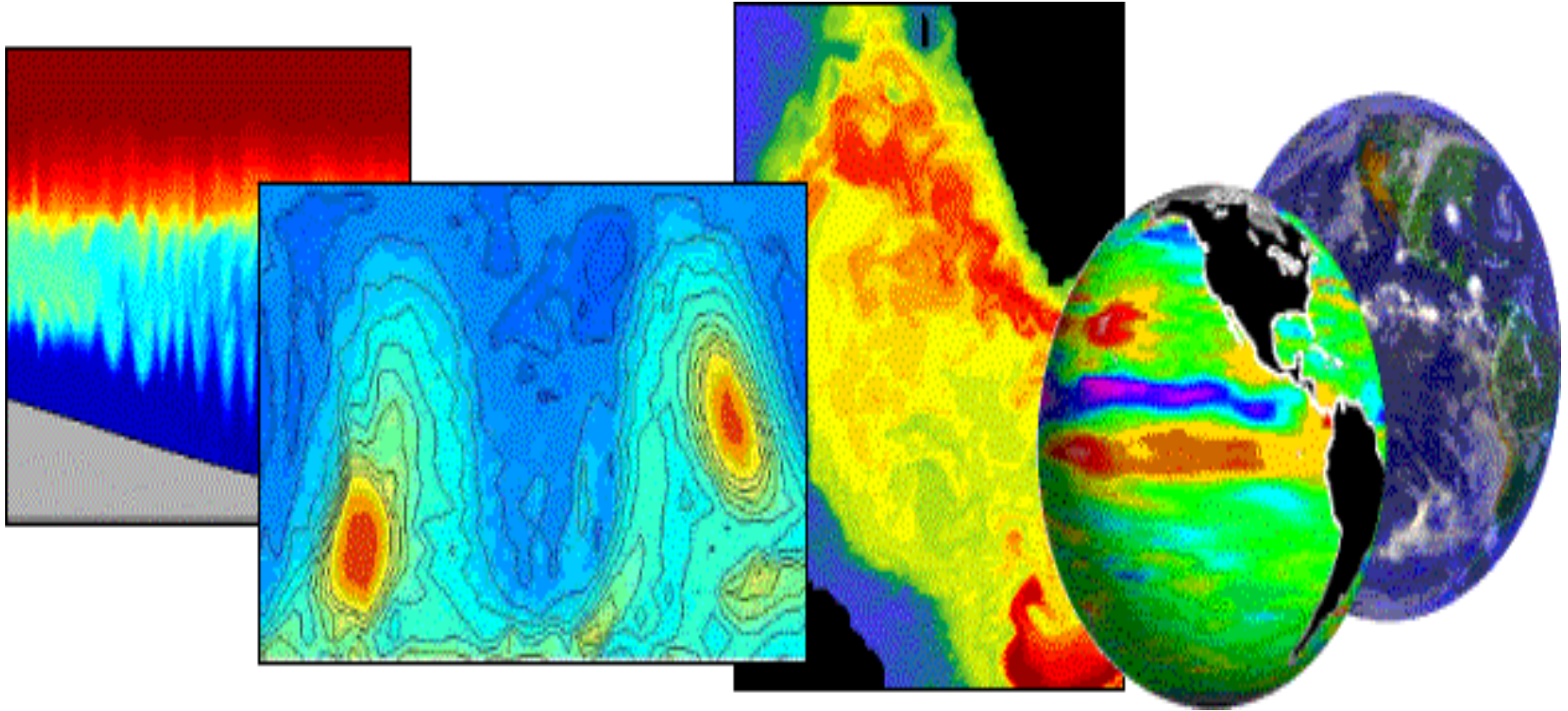
## Introduction: Approaches to oceanic studies



**Ansong & Sutherland (2010), JFM, vol 648**



# Introduction: Approaches to oceanic studies



**Ocean modeling**

**Riccardo/Brian/Dimitris/Joseph**

# What is an ocean model?

It is a **representation**, in the form of **equations/computer code**, describing **physical processes** of our understanding of how the ocean works.

**-Dr. Stephenie Waterman**

# What is an ocean model?

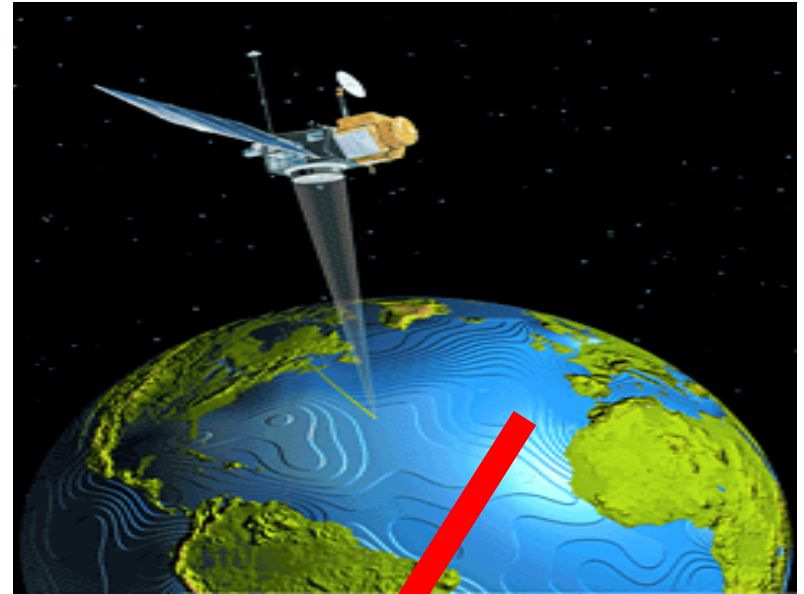
## Physical processes:

- a) Ocean movement/dynamics, including horizontal and vertical advection
- b) Exchange of energy between the ocean and external sources (radiation, precipitation, evaporation, river-runoff, wind, etc)
- c) 3D mixing and dissipation processes

# QUESTION

**Why do we need ocean modeling when we have alternative means?**

# Motivation: Why model the ocean?



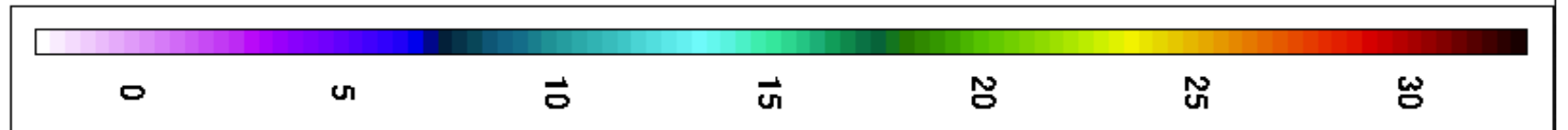
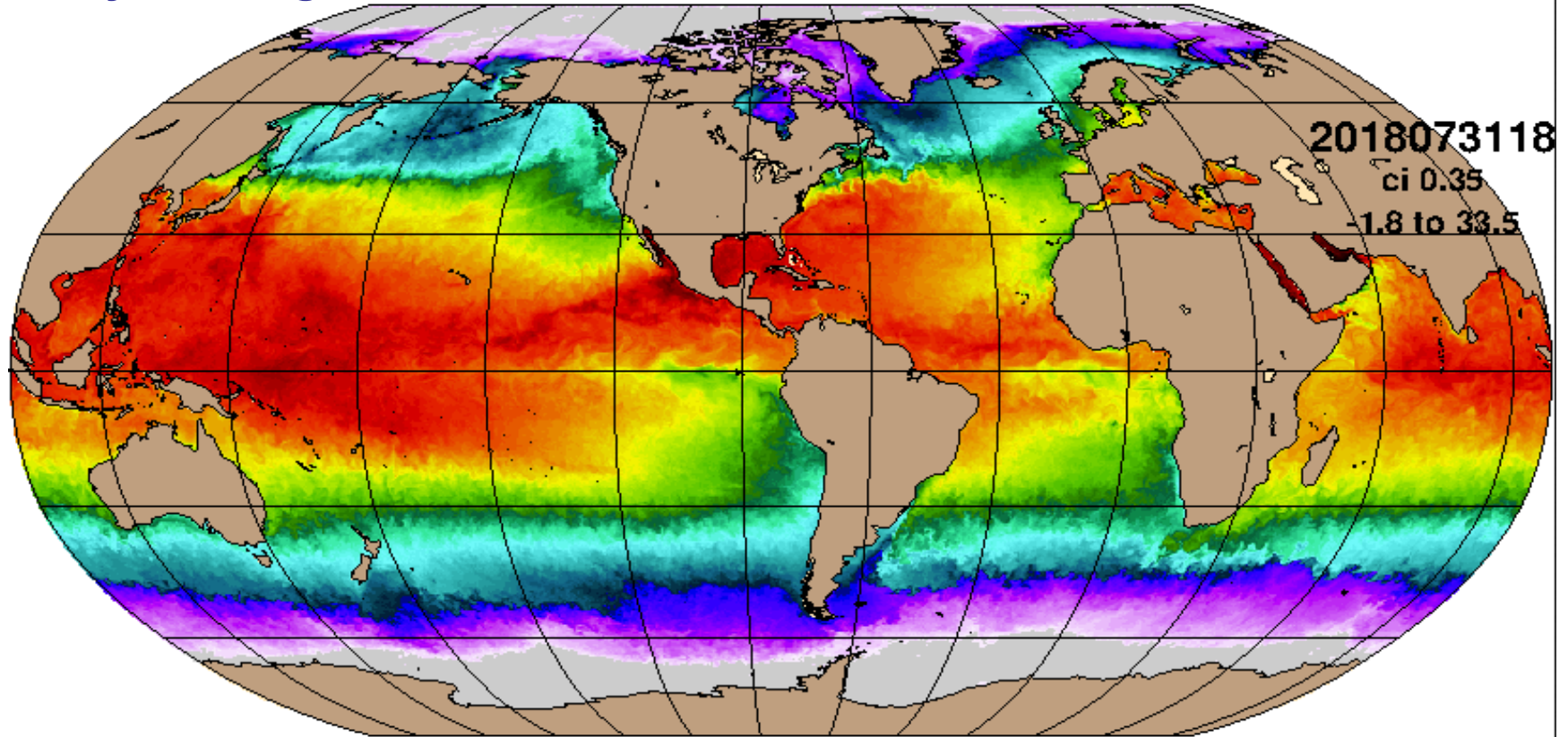
# Motivation: Why model the ocean?

- Comparatively less expensive
- Higher spatial/temporal resolution compared to other methods:
  - Satellites provide only surface data, and
  - In-situ measurement are limited in spatial coverage
- Ability to forecast (e.g. SST, SSH, and positions of major fronts and eddies)

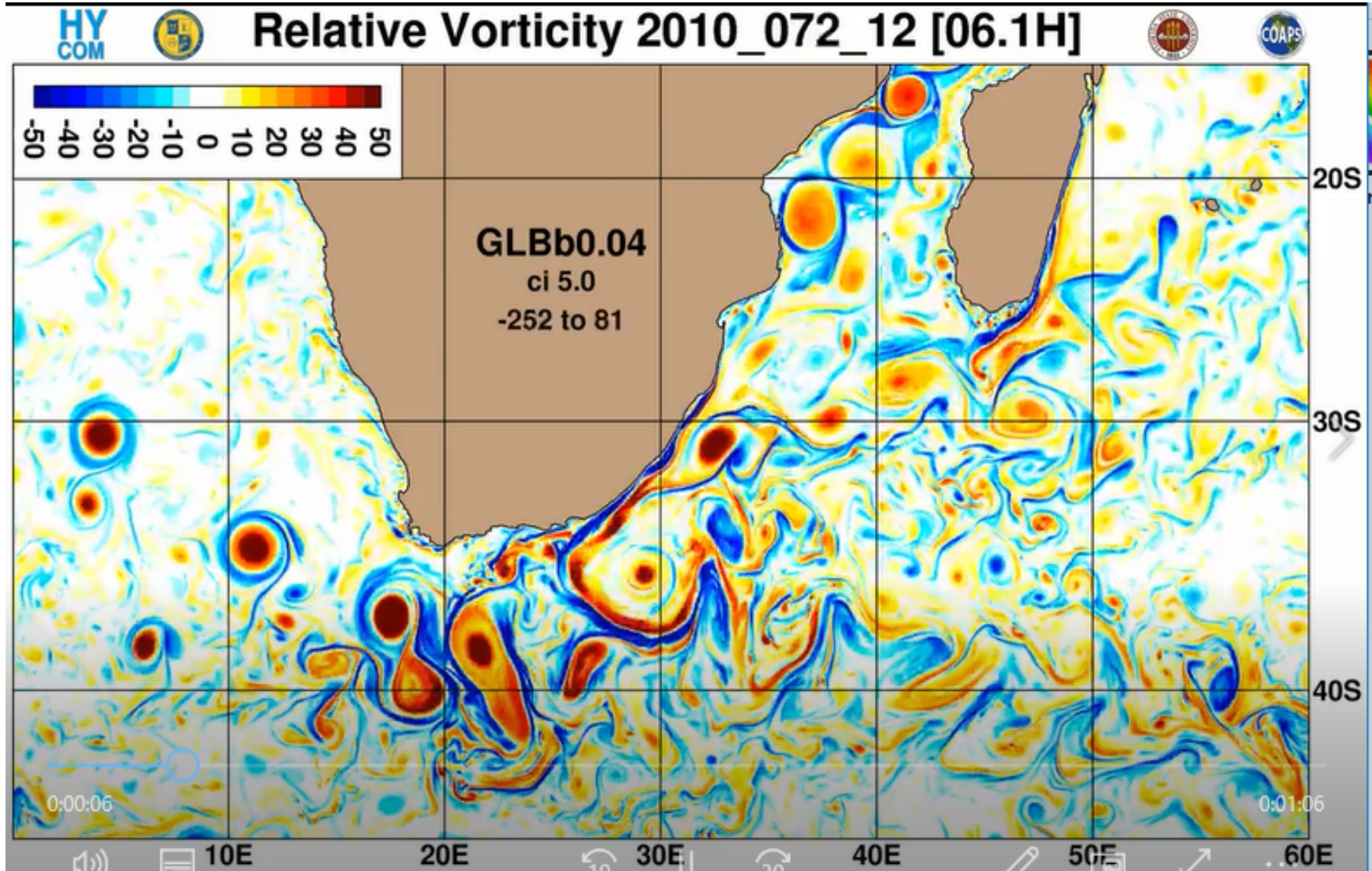
# Motivation: Why model the ocean?

[www.hycom.org](http://www.hycom.org)

SST Aug 05, 2018 00Z 91.2

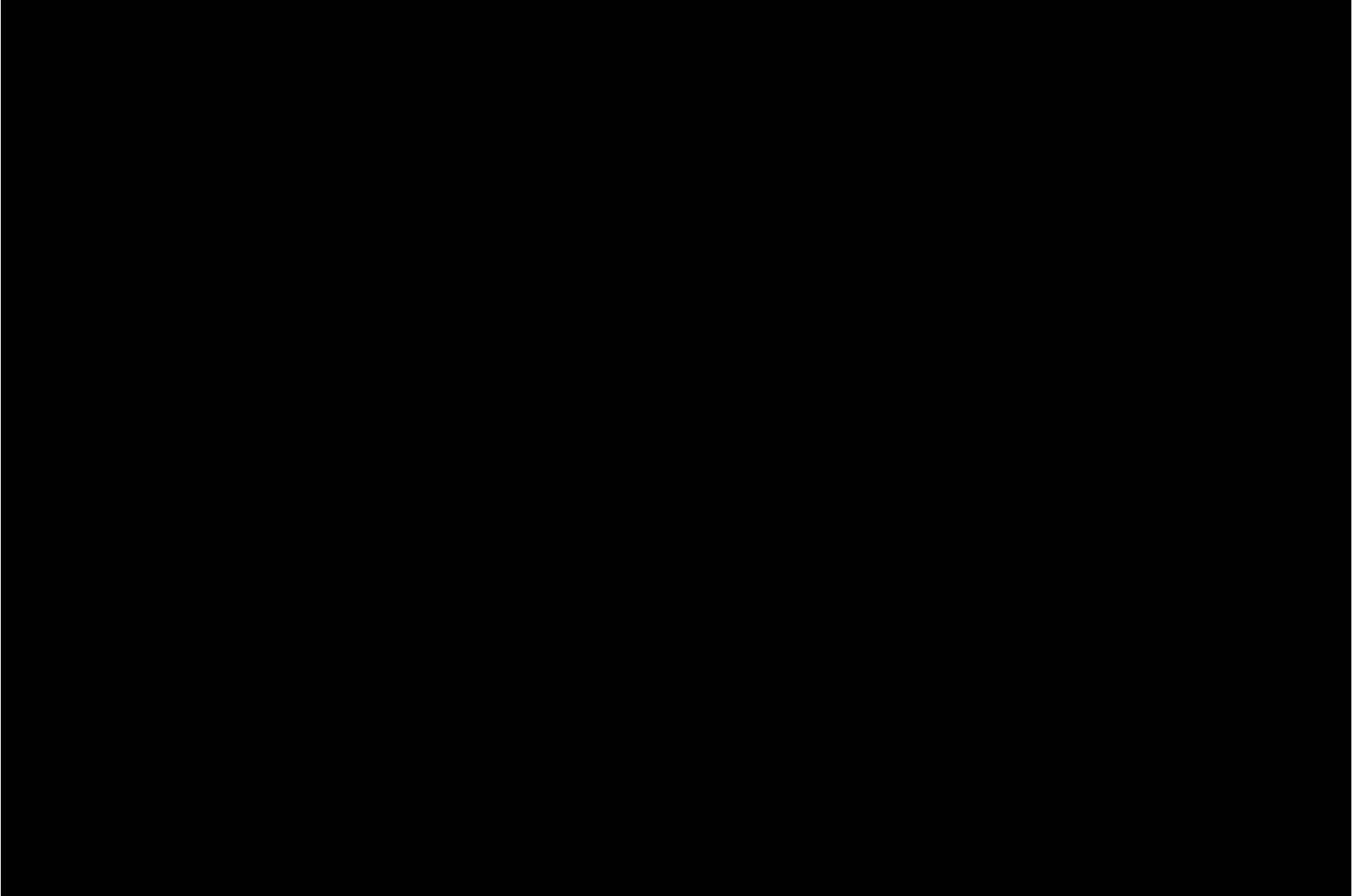


# Motivation: Why model the ocean?



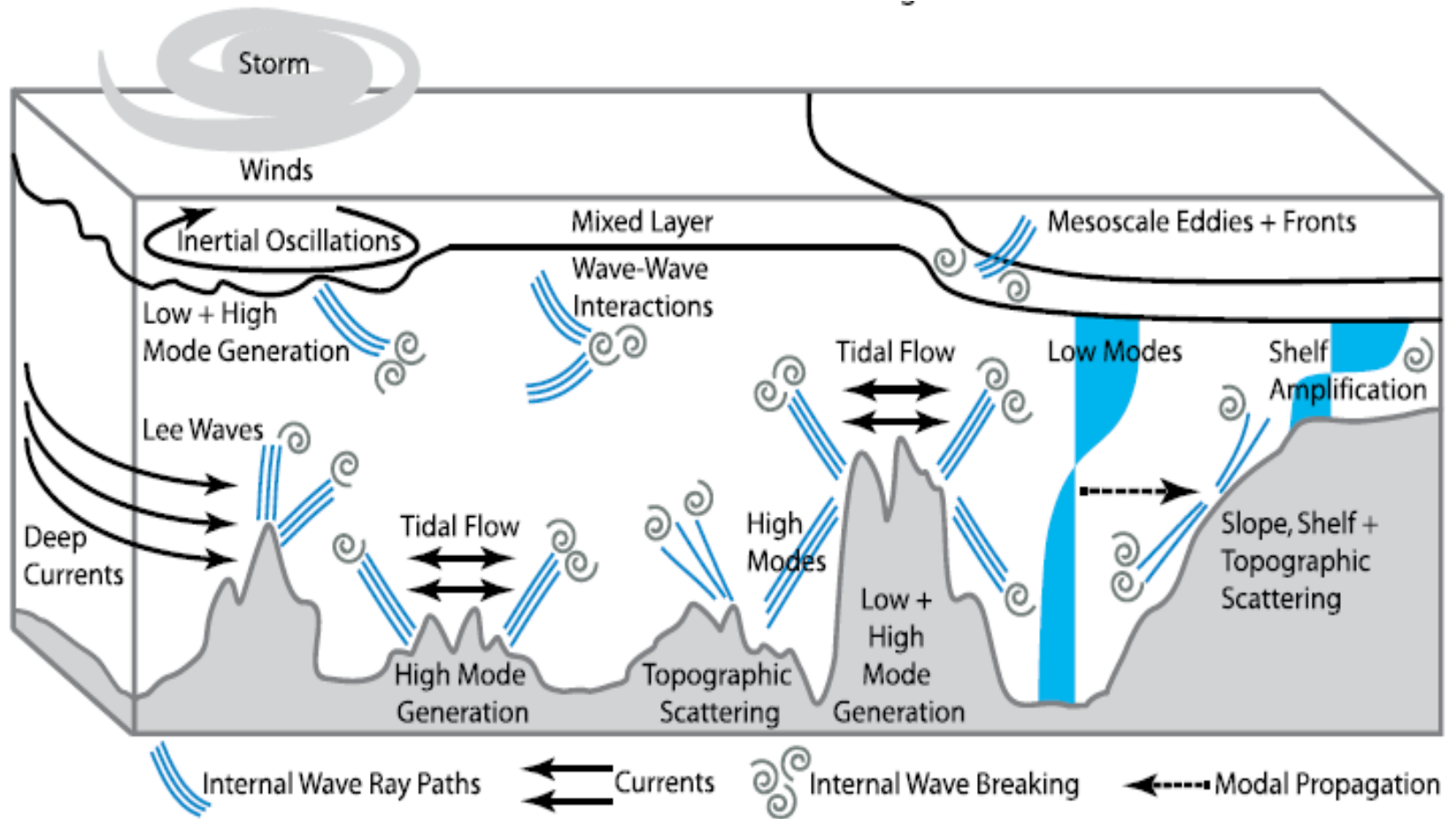


# Motivation: Why model the ocean?

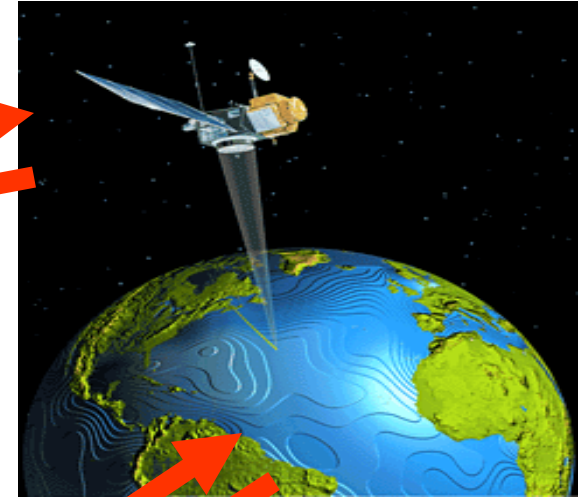


# Motivation: Why model the ocean?

Understanding the 3D dynamics of the ocean on a GLOBAL scale.

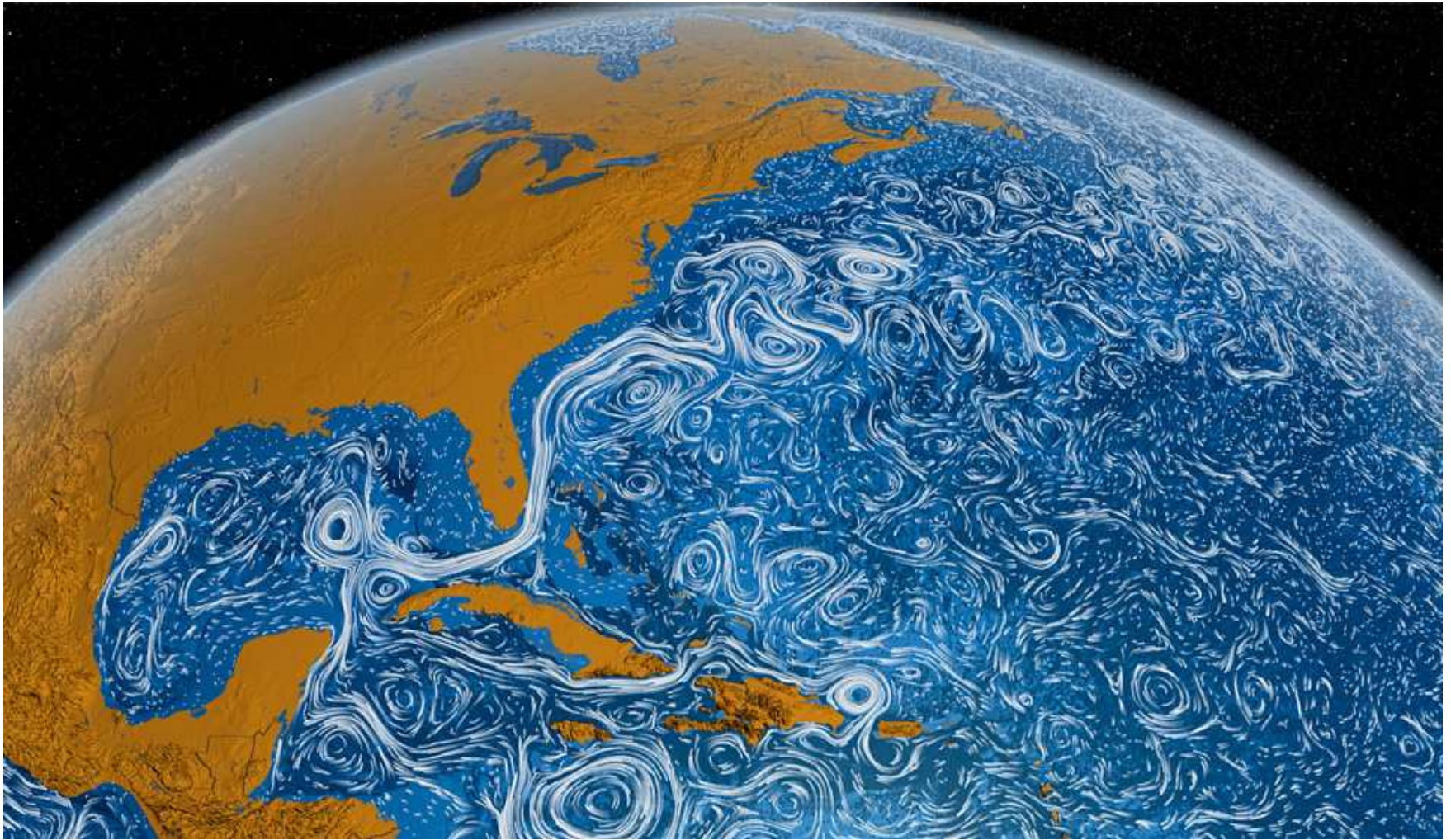


# Motivation: *not a competition*

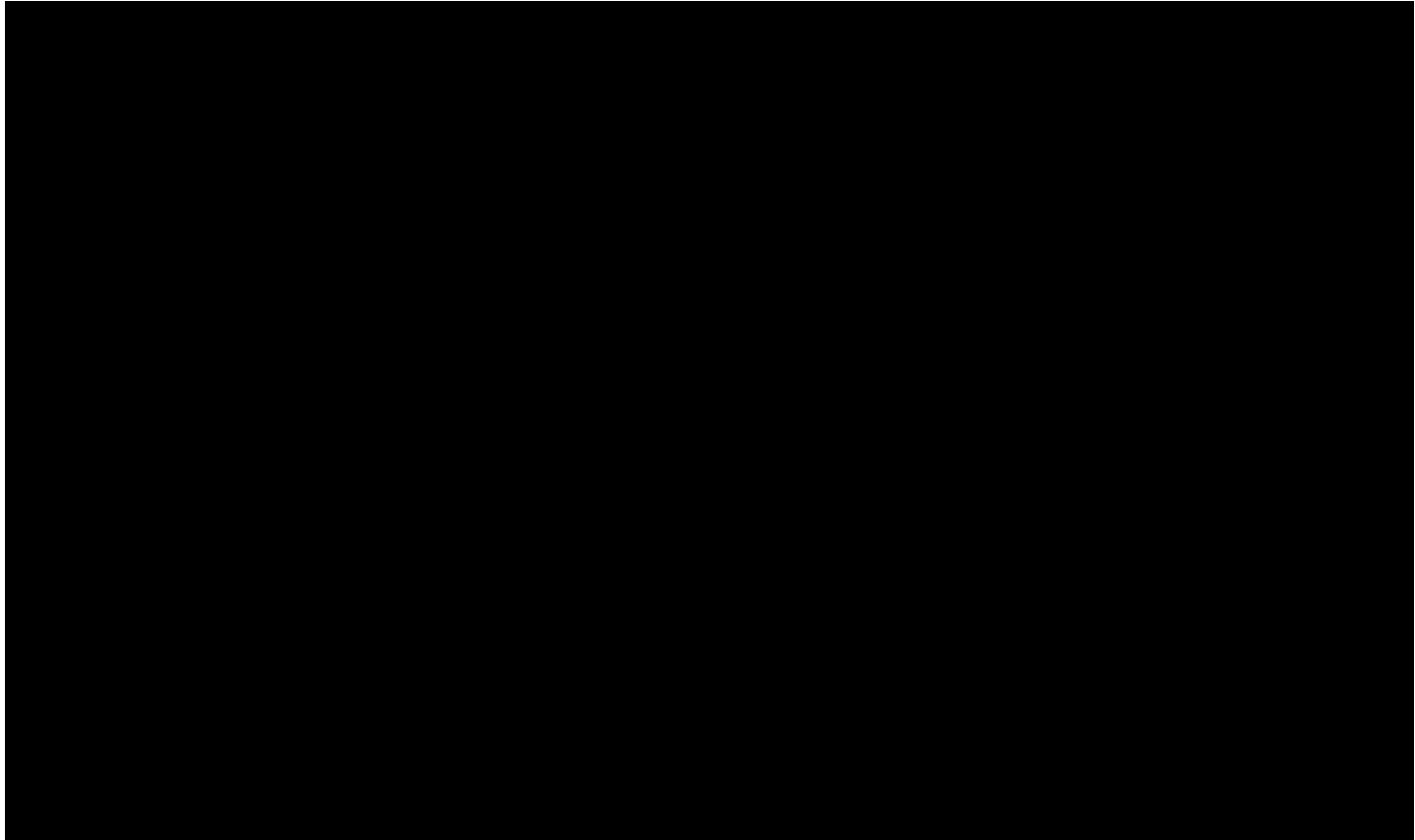


**Prof. Modeller**

# Motivation: global ocean currents

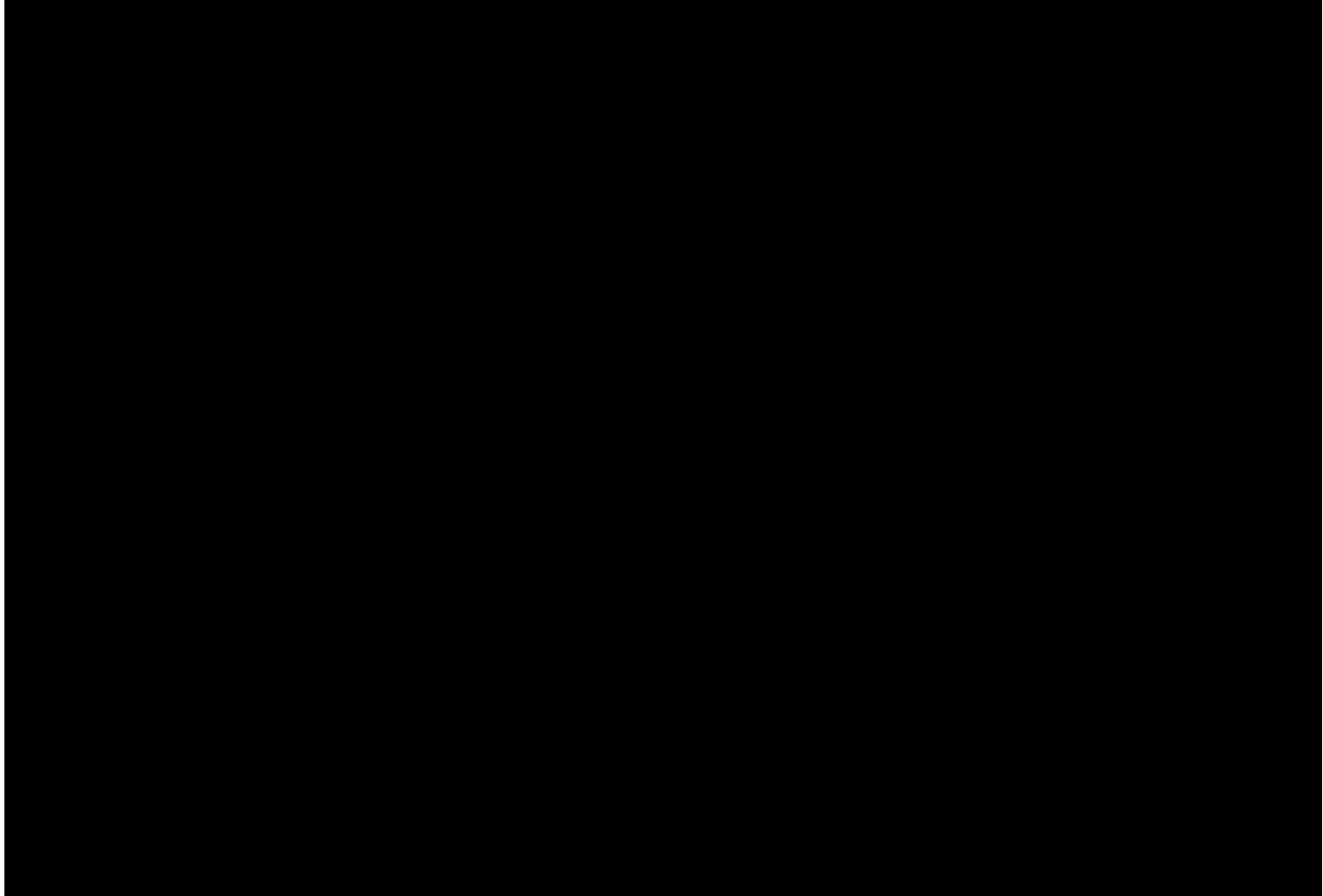


# Internal gravity waves



**Generation of Internal gravity waves by sinusoidal hills  
(Prof. Bruce Sutherland)**

# Motivation: internal waves



**Courtesy: Max-Planck institute of Ocean modeling**

**Where/how do I start  
learning ocean modeling?**

# Definition: ocean model

It is a **representation**, in the form of **equations/computer code**, describing **physical processes** of our understanding of how the ocean works.

**-Dr. Stephenie Waterman**



# Equations of motion

- Start ocean modeling by understanding the equations of fluid flow (Navier-Stokes equations).
- Learn how to discretize the equations
- Understand some numerical analysis
- Others...

# Equations of motion:

$$\frac{D\vec{u}}{Dt} + 2\vec{\Omega} \times \vec{u} = -\frac{1}{\rho_0} \nabla p + \frac{\rho}{\rho_0} \vec{g} + \vec{F}$$

acceleration  
(local +  
advective)

Rotation

Pressure  
gradient

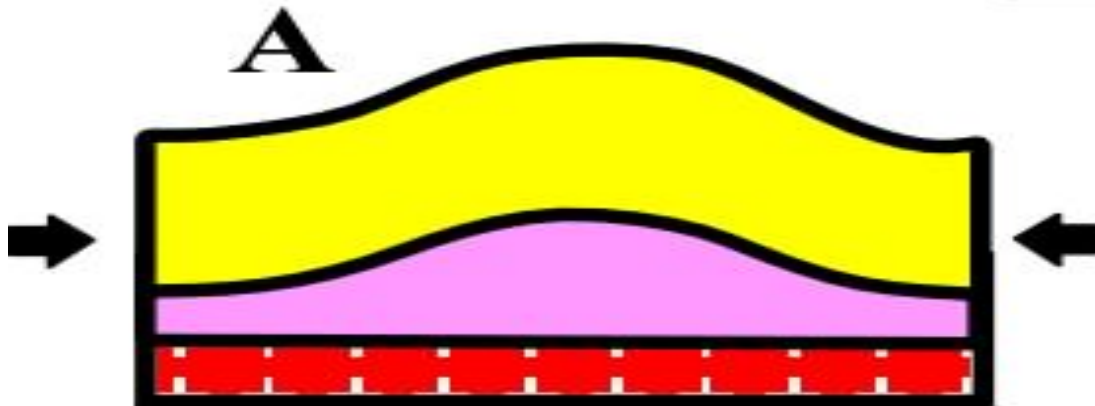
buoyancy

Others  
(frictional,  
Tides,  
Winds, etc)

where ( $\mathbf{u}=[u,v,w]$ ) are velocity components,  $\Omega$  is the earth's rotation rate,  $p$  is the pressure,  $\rho$  the density, and  $g$  gravity.

# Continuity equation (Conservation of volume)

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} + \frac{\partial w}{\partial z} = 0$$

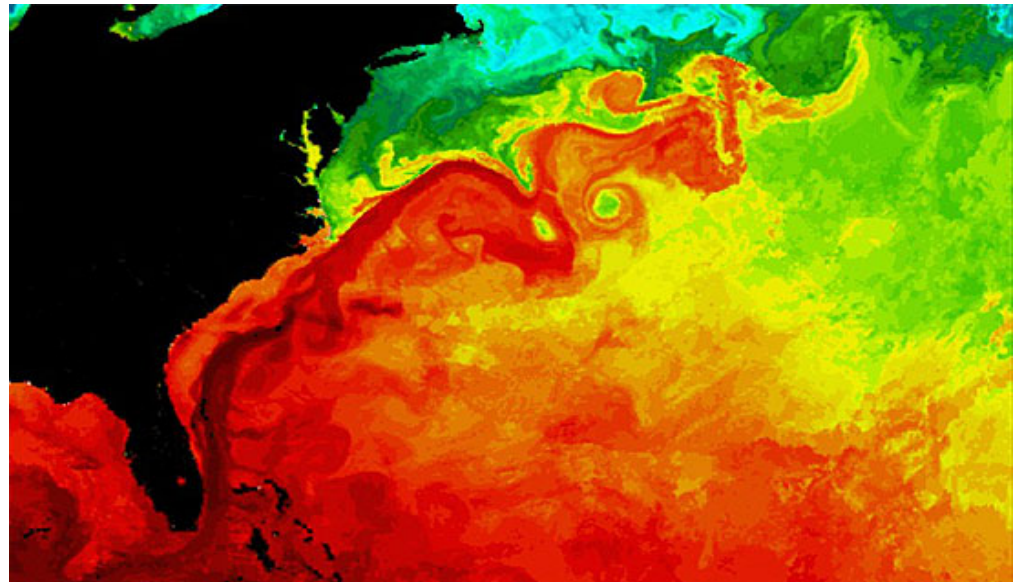


## Equation for tracers (Temperature, Salinity, and others),

Advection-diffusion equation:

$$\frac{\partial T^c}{\partial t} + \mathbf{u} \cdot \nabla T^c = \kappa_{T^c} \nabla^2 T^c$$

$T^c = \textit{Tracers}$



# Equation of state (Linear)

$$\rho = \rho_0[1 - \alpha(T - T_0) + \beta(S - S_0)]$$

$$\rho_0 = 1028 \text{ kg / m}^3 \quad \text{coefficients of thermal, } \alpha,$$

$$T_0 = 10^\circ \text{ C} = 283 \text{ K} \quad \text{and saline contraction, } \beta$$

$$S_0 = 35 \text{ psu}$$

Where T is temperature and S is salinity.

# Equations of motions

7 equations in 7 unknowns:

- $\{u,v,w\}$  – 3 velocity components
- T – Temperature
- S – Salinity
- Density
- P – Pressure

Now that I understand the  
equations, what next?

A. Discretize equations

B. Consider the horizontal grid

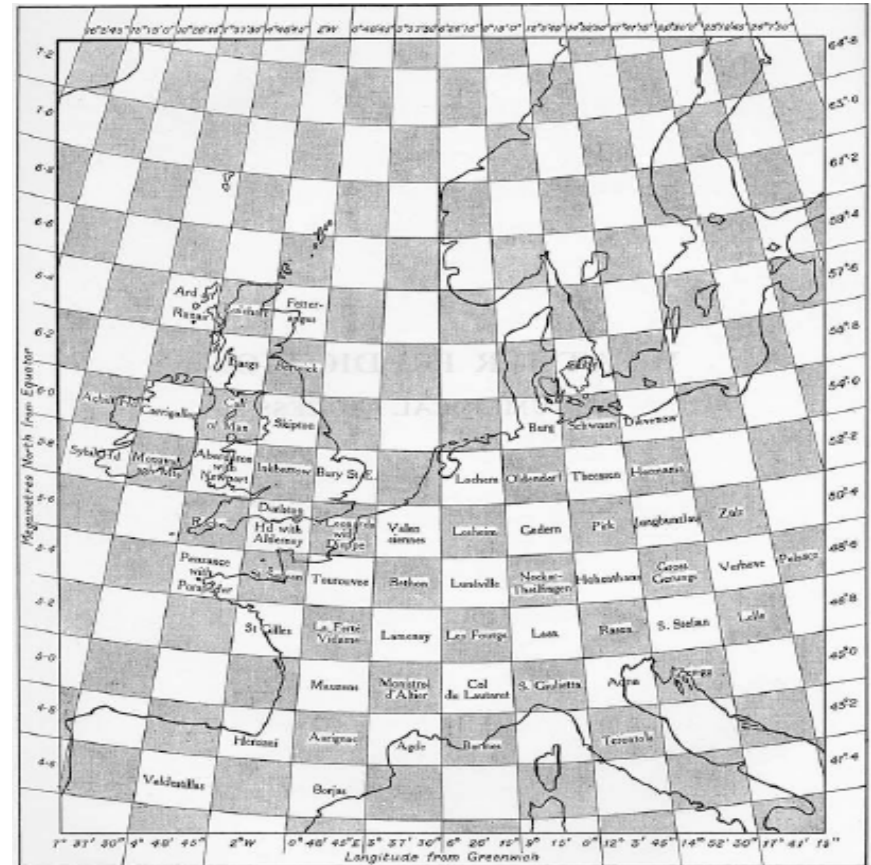
C. Consider the vertical grid

D. Boundary conditions



# Discretize equations

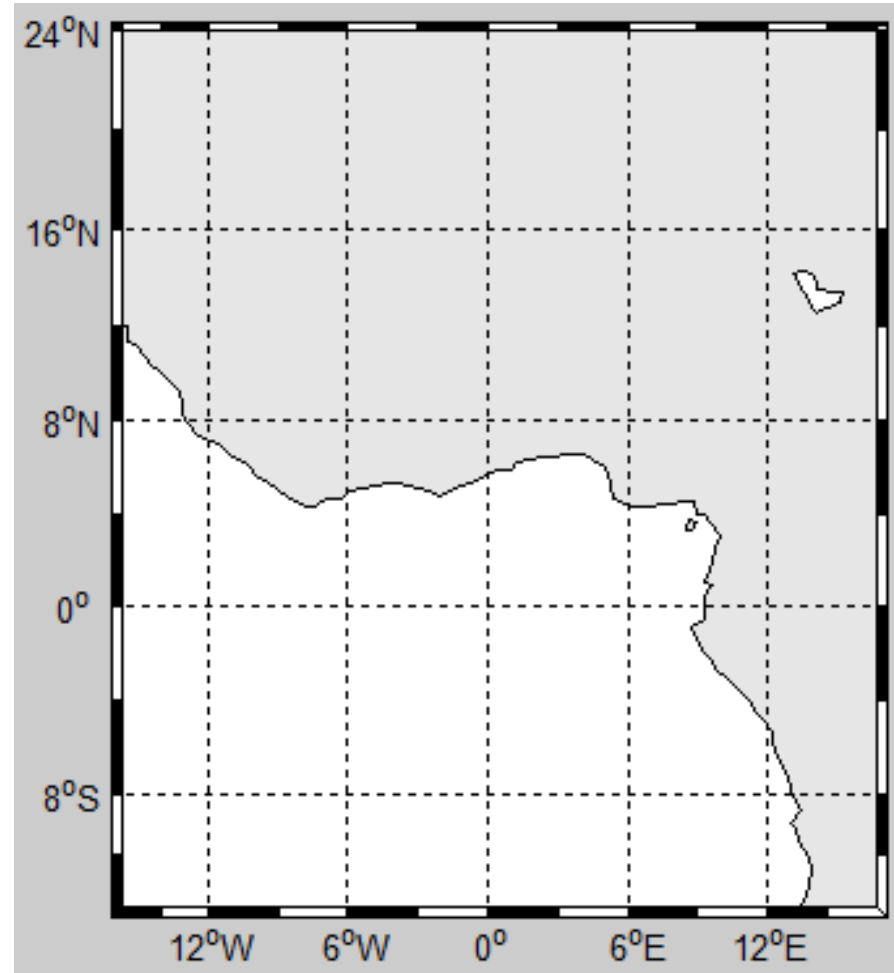
- Continuous equations  
↓  
algebraic equations  
(discrete set of operations)
- Discretization methods:
  - Finite difference methods
  - Finite element methods
  - Finite volume methods



**Example early model grid by Lewis Fry Richardson (1928)**

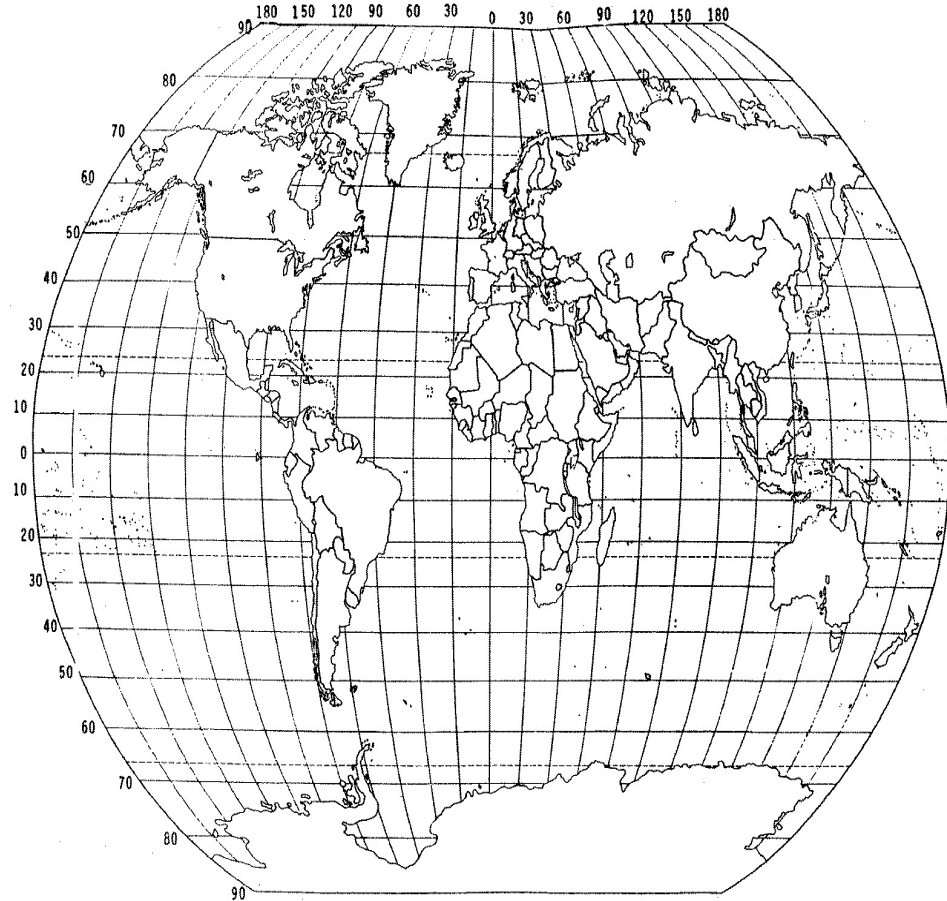
# Model grid: horizontal

- Regular grids: regularly spaced lines
- possible in a small domain

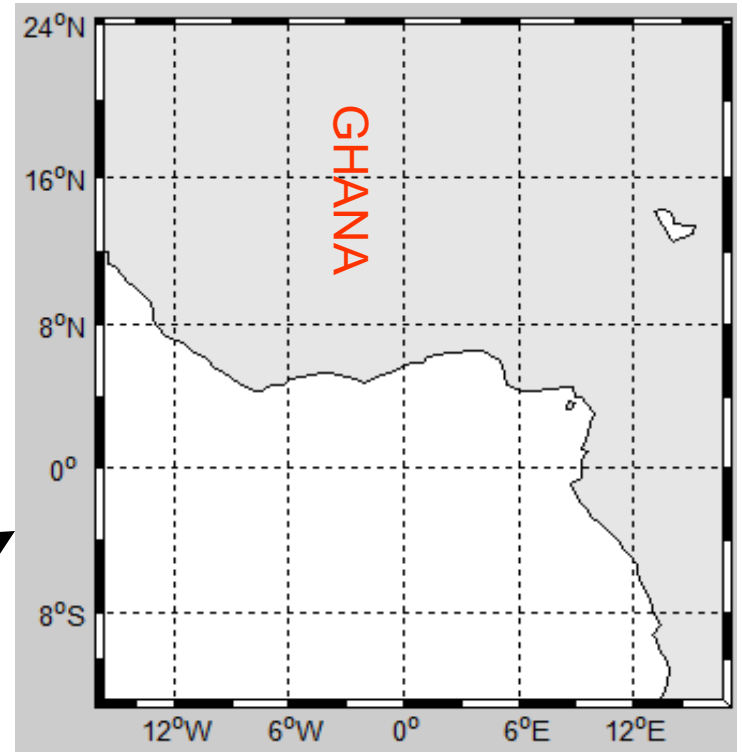
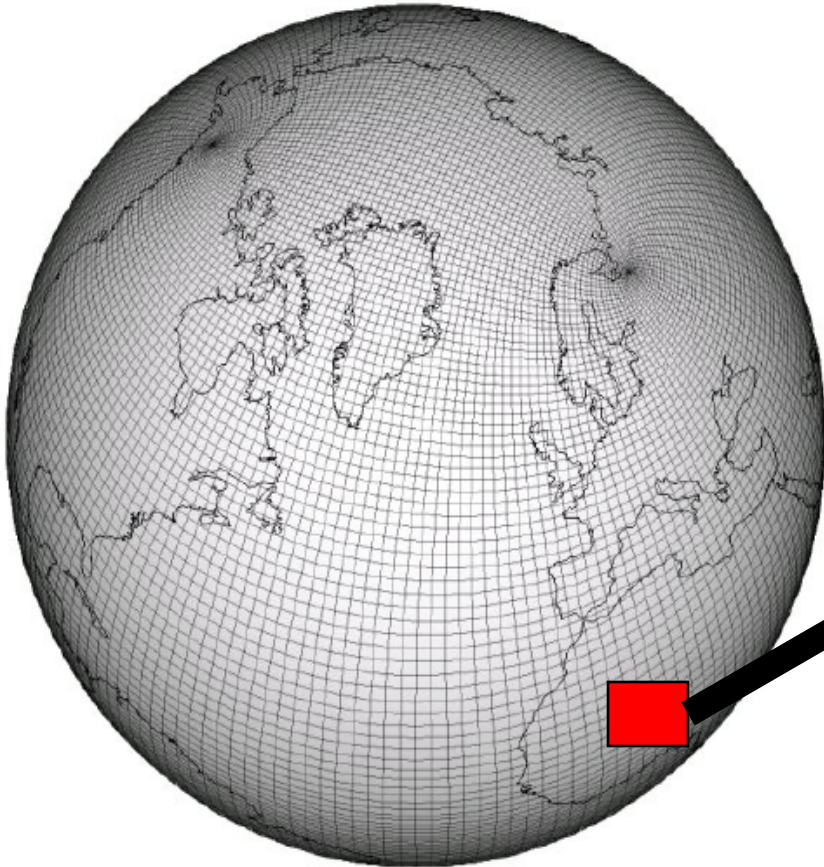


# Model grid: horizontal

- **Regular grids:** regularly spaced lines
- On a spherical earth can't have both uniform grid spacing and straight lines
- Regular lat/lon grids have a problem at the poles where grid lines converge



# Model grid: horizontal



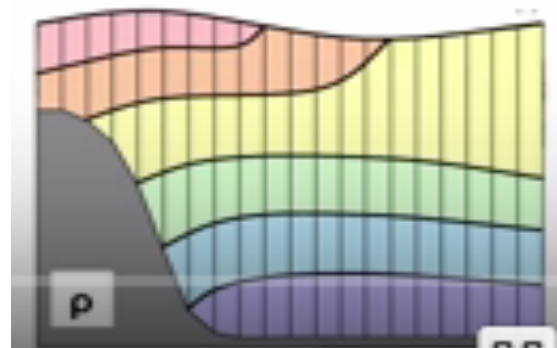
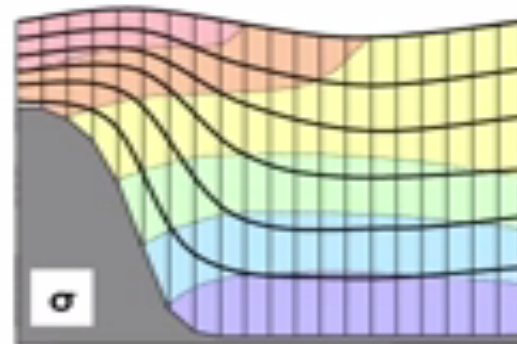
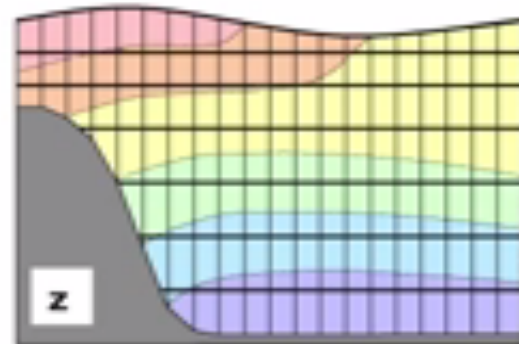
Regional grid

Clever solution: tripolar grid

-circular grid laid over Arctic region with poles on land

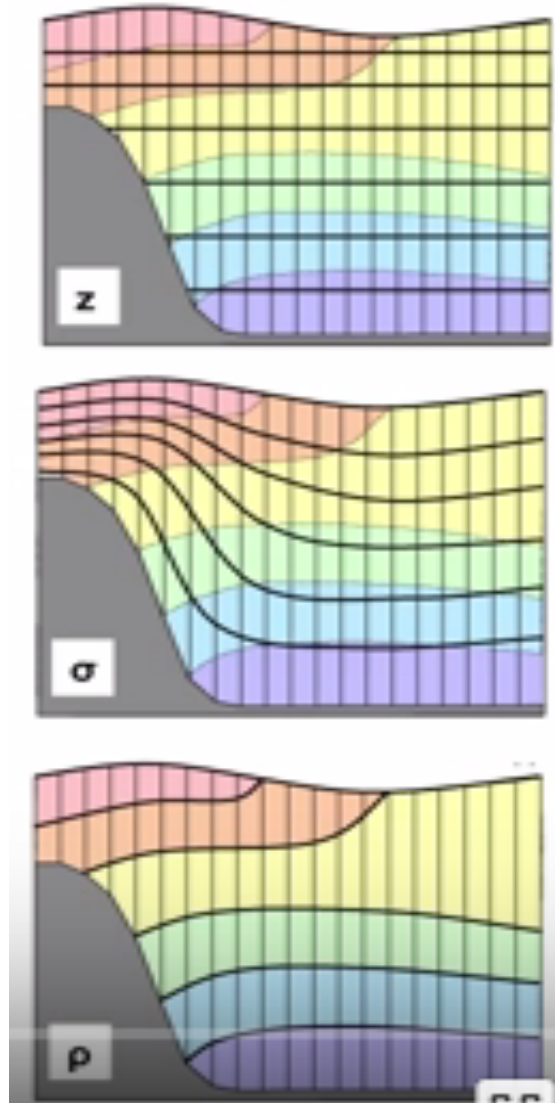
# Model grid: vertical

- **z-coordinate** system based on a series of depth levels. Easy to setup. Difficult to locally increase resolution.
- **terrain-following** coordinate system. Mimics bathymetry and allows higher resolution near ocean floor.



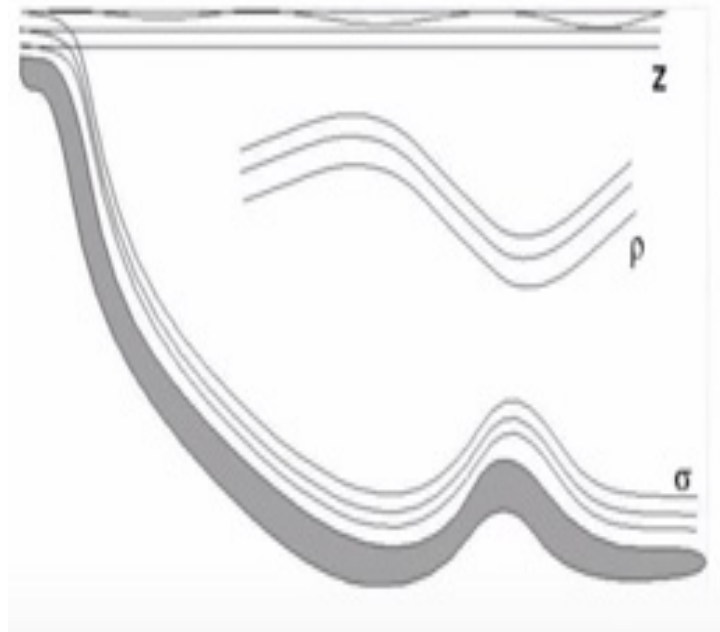
# Model grid: vertical

- density (isopycnal)-coordinate system based on density layers. Great in the deep ocean where there's less diapycnal mixing. Poor in regions with high vertical mixing.



# Model grid: vertical

- **hybrid-coordinate** applies the best suited coordinate system in different regions. Gives improved results but at a high computational cost.



# Boundary conditions

- Free surface
  - Flux exchanges at surface: momentum and tracer (winds, solar radiation, rainfall, precipitation, etc).
- Ocean bottom
  - Topography/bathymetry
  - Velocity normal to bottom is zero
  - Lateral boundaries (open/closed)
- Flow normal to solid boundary is zero

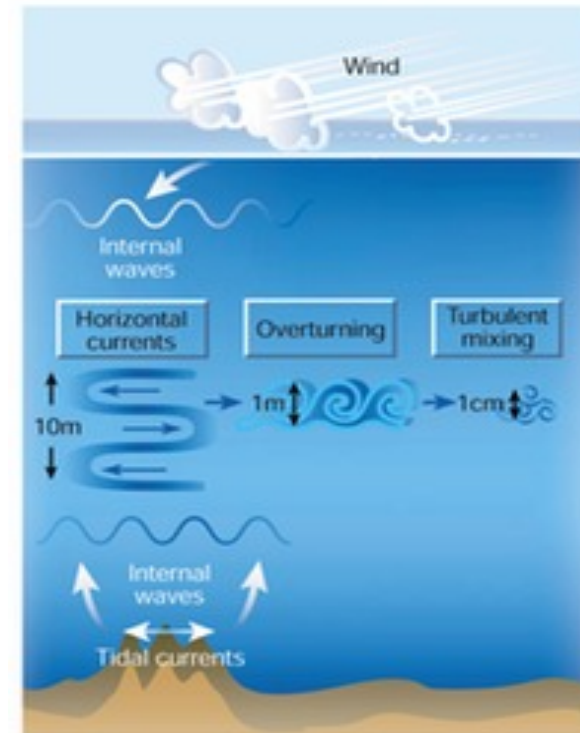
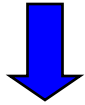


Figure 1. Internal waves and their effects on ocean currents.

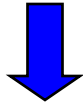


# Modeling: summary

- Complex differential equations



- Set of algebraic equations



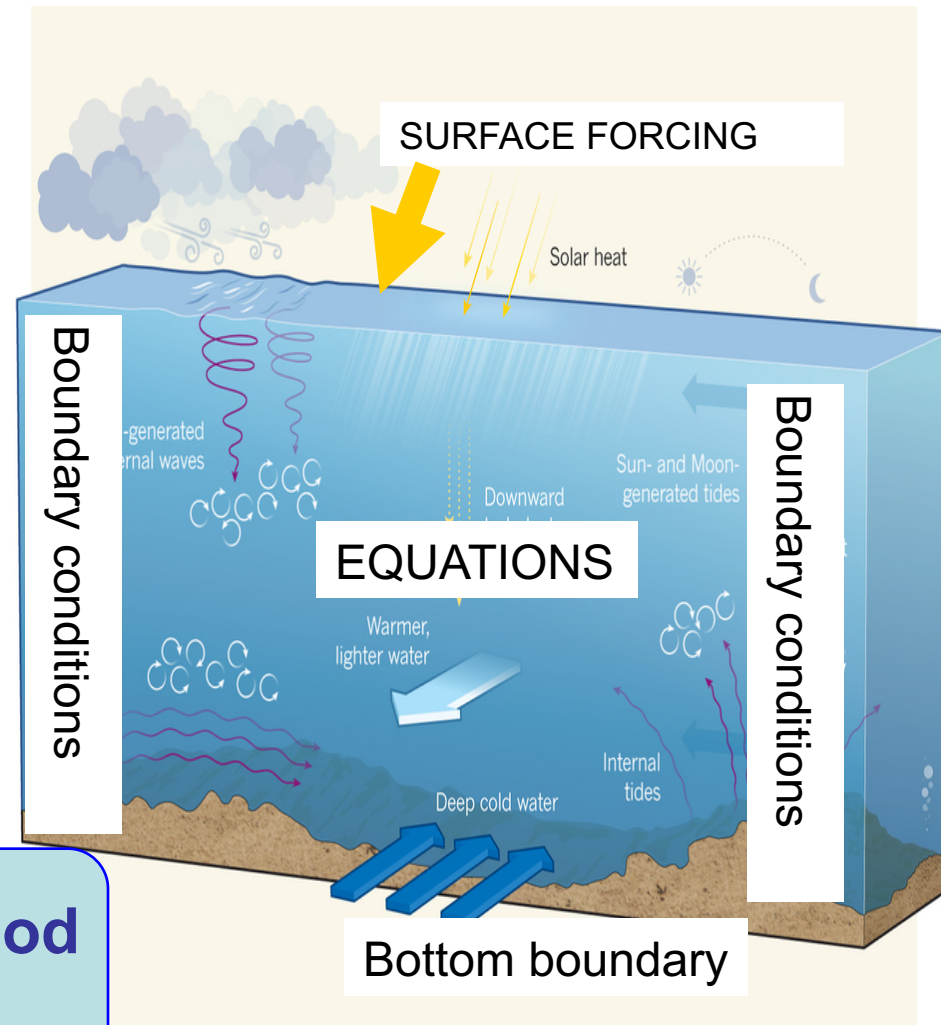
- Step-by-step method of solution

(model time stepping)

at selected points in space

(model spatial grid)

**It takes years to develop a good ocean model!**



# Ocean models

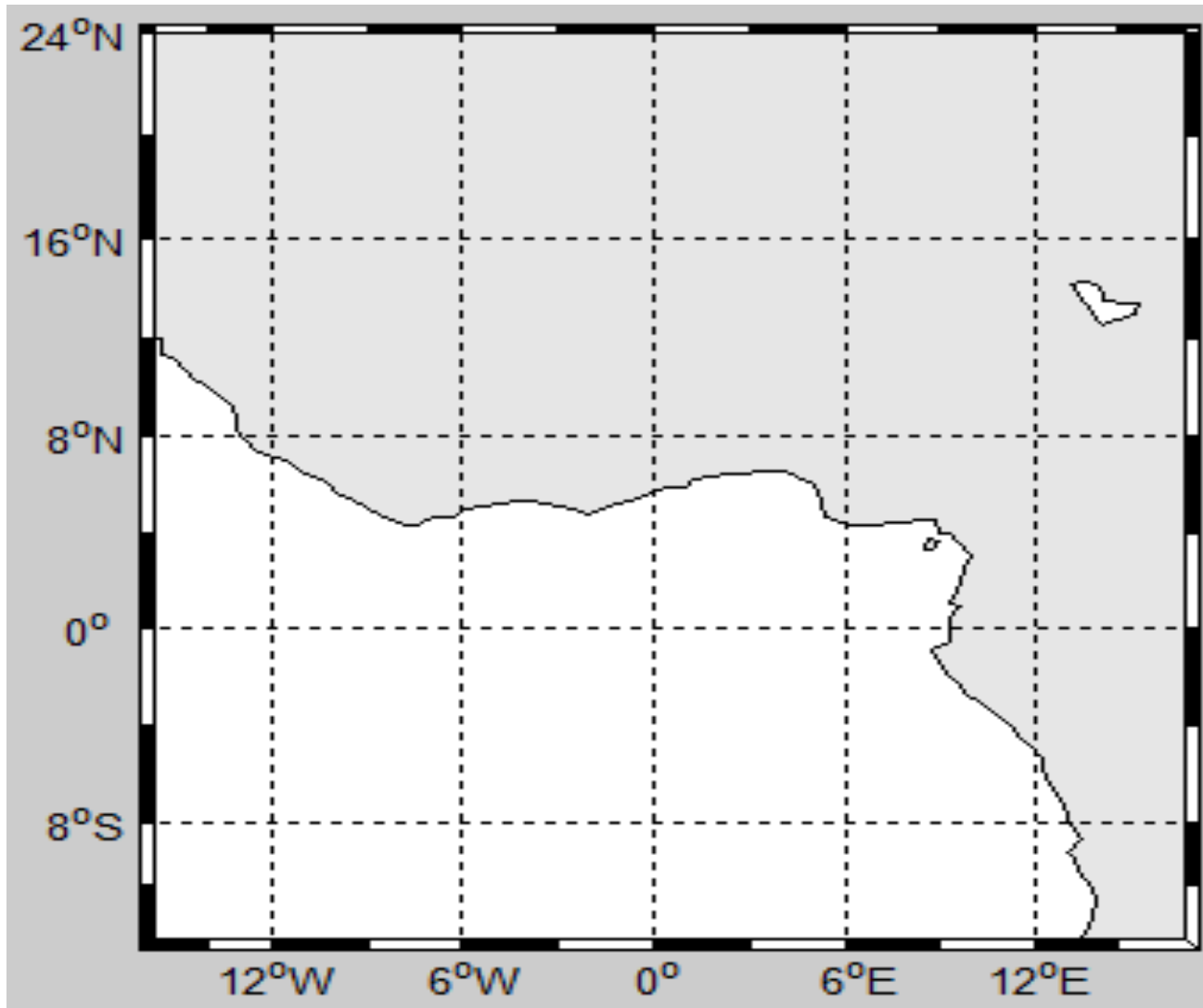
- MOM (The Modular Ocean Model: <http://mom-ocean.org/web> )
- POM (The Princeton Ocean Model: <http://www.ccpo.odu.edu/POMWEB/> )
- POP (The Parallel Ocean Program: <http://www.cesm.ucar.edu/models/cesm1.0/pop2/> )

# Ocean models

- MITgcm (MIT general circulation model: <http://mitgcm.org/> )
- HYCOM (The Hybrid Coordinate Ocean Model : <https://hycom.org/> )
- ROMS (Regional Ocean Modeling System: [www.myroms.org](http://www.myroms.org) )

# Examples

# Regional Modeling

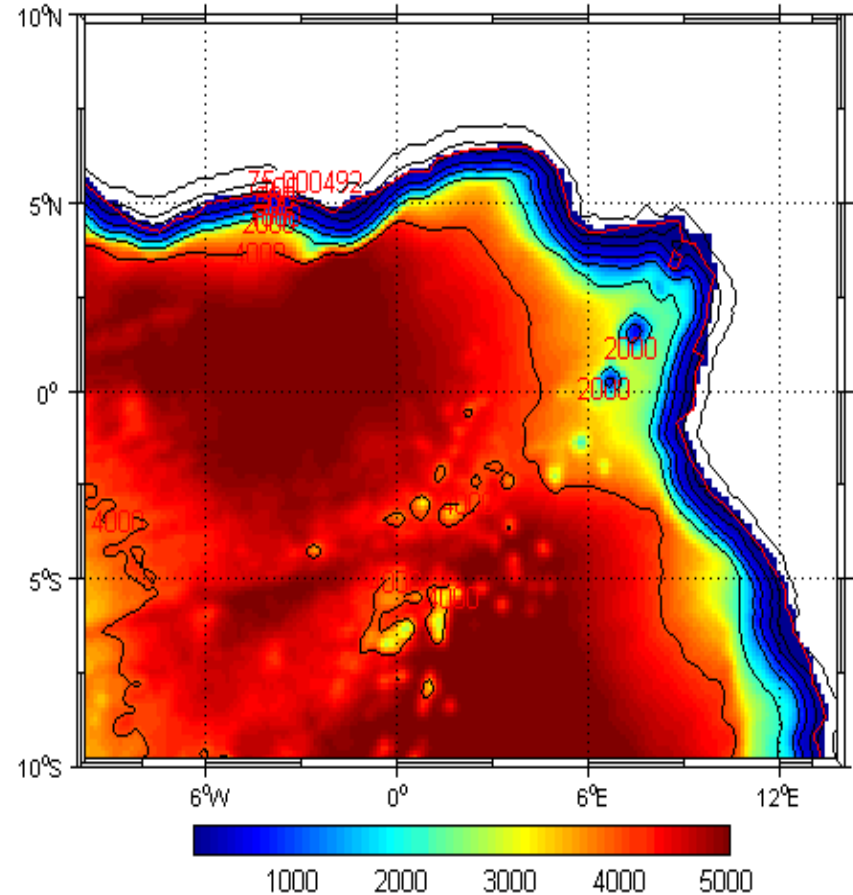
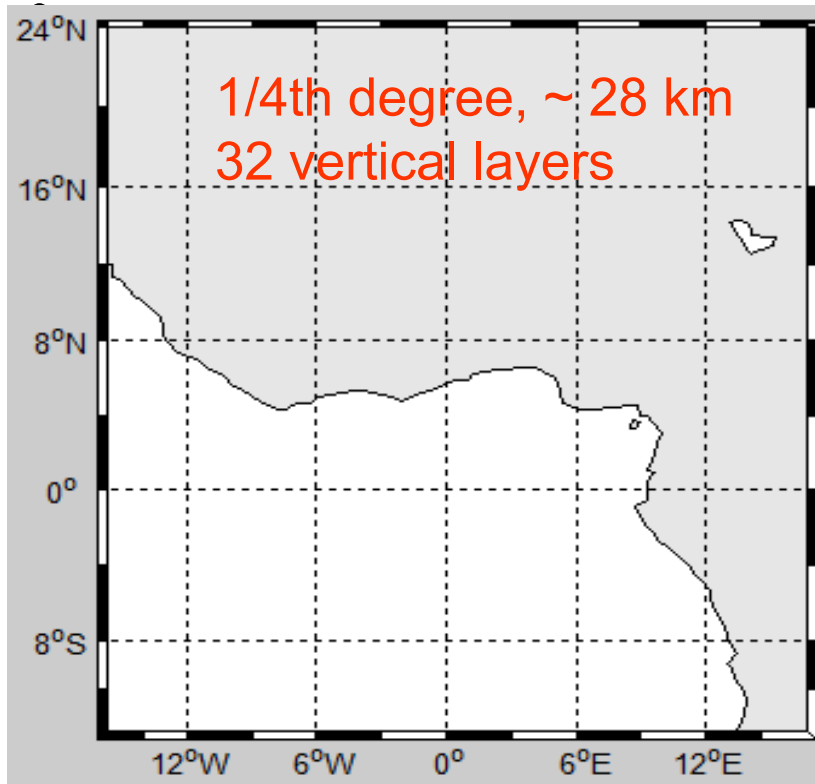


# Regional Modeling

## Operational Guidelines:

1. Choose a domain and resolution.
2. Build a bathymetry.
3. Interpolate atmospheric forcing to the domain.
4. Choose vertical structure
5. Interpolate T/S climatology to the model domain
6. Run the simulation.
7. Plot and analyze results.

# Regional Modeling

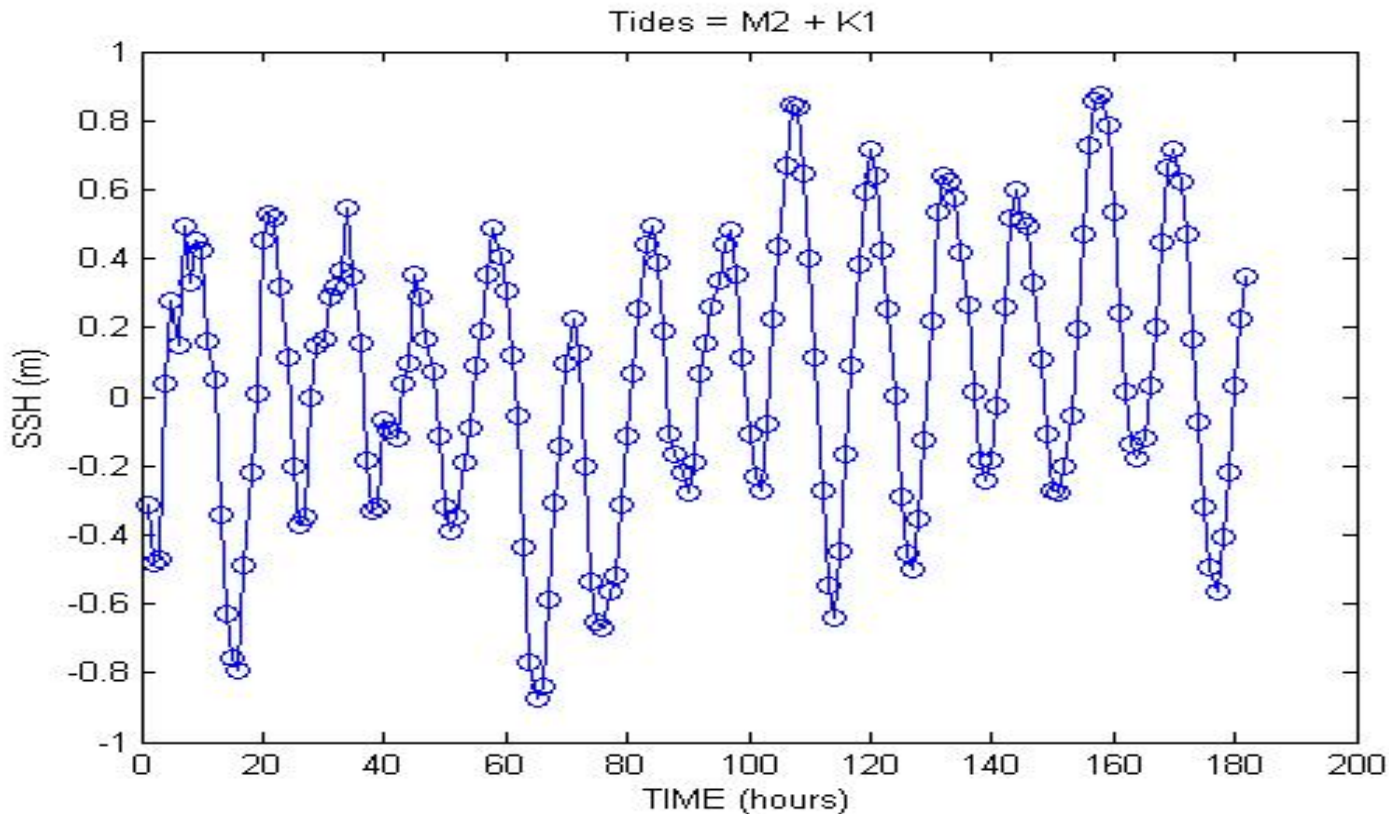


Etopo5: <http://www.ngdc.noaa.gov/mgg/global/etopo5.HTML>





# Results: tidal time series



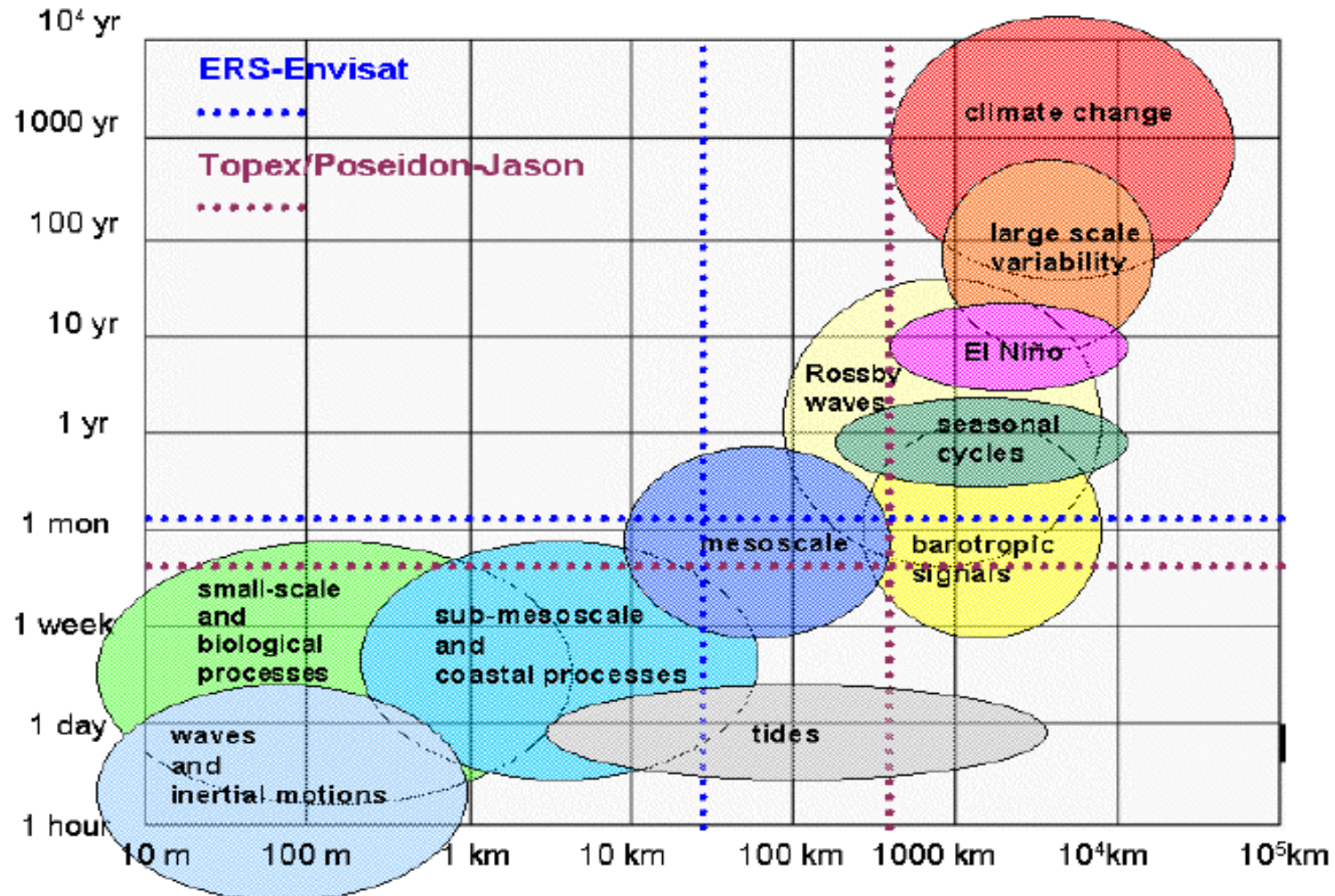
**Challenge: compare to tide-gauge data (Takoradi/Tema)**

# Challenges to ocean modeling

What are some challenges?

# Challenges to ocean modeling

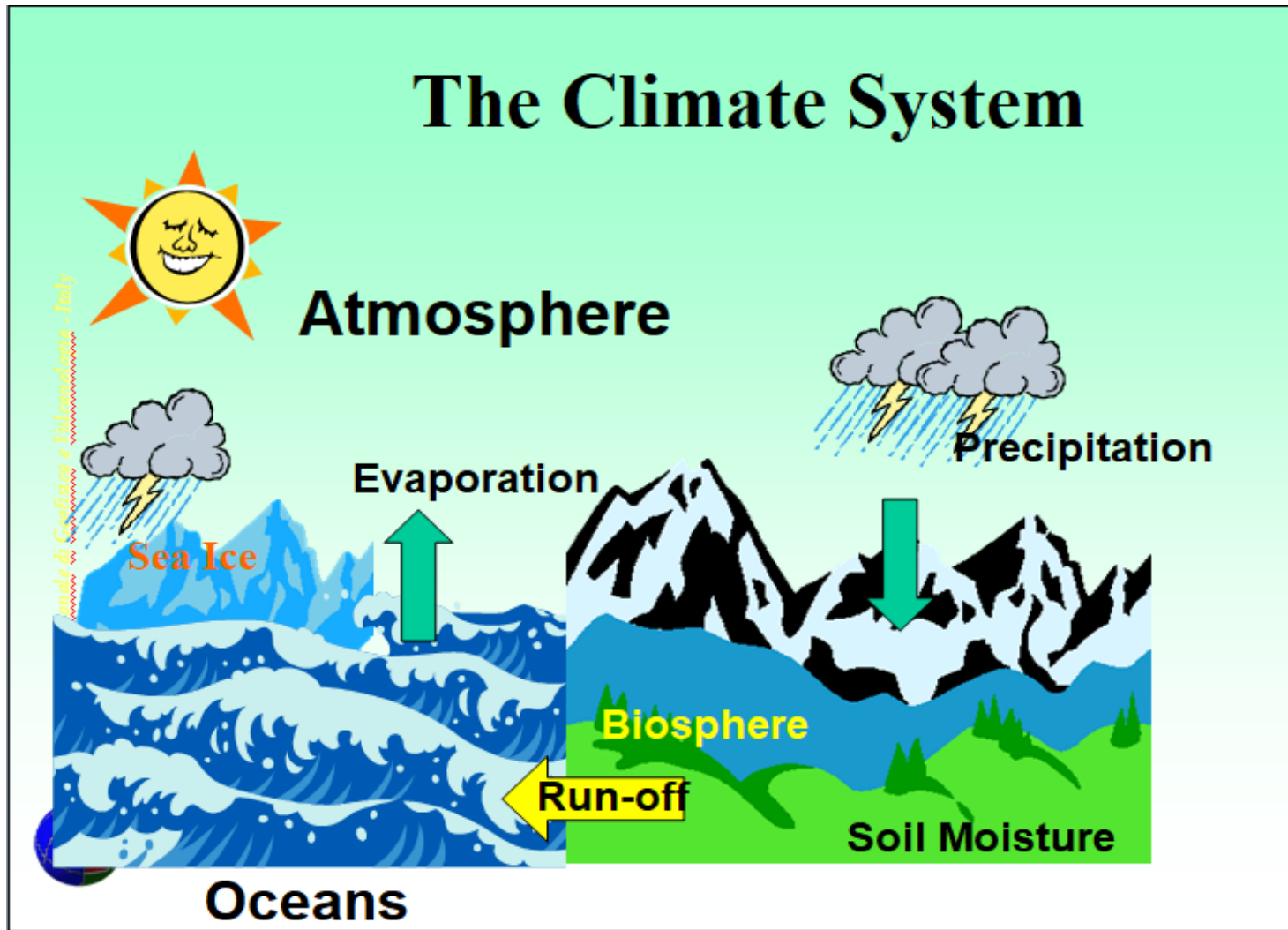
## 1. Variable spatial/temporal scales



# Challenges to ocean modeling

## 2. Coupling the Atmosphere to the Ocean

Antonio Navarra



# Challenges to ocean modeling

3. Complex topography and lateral boundaries
4. Few observational measurements for validation
  - most available data are confined to upper ocean
5. Availability of computational power

**QUESTIONS?**