

Ocean circulation models and modelling: A General Overview

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Outline

- 1 Outline and aims
- 2 Motivation for using ocean models
- 3 Posing the ocean model problem
 - A sample of ocean processes
 - The ocean parameterization problem
- 4 The vertical
- 5 The horizontal
- 6 Where we are
- 7 References and further reading

Outline

1 Outline and aims

Two pillars of numerical oceanography

- OCEAN MODELS:
 - Repository for mechanistic theories of how the ocean works, with numerical methods transforming theories into a computational tool for scientific investigations.
 - Mathematically formulated physical theories and numerical methods provide the foundation.
- OCEAN MODELLING:
 - The use of numerical simulations as an experimental tool to help deduce mechanisms for emergent space-time patterns of ocean phenomena.
 - Math physical theories and analysis methods provide the foundation.

Topics to be discussed

- Science of ocean models
 - continuum thermo-hydrodynamical equations
 - algorithms for hydrostatic primitive equations
 - subgrid scale parameterizations
- Science from ocean models (ocean modelling)
 - analysis of heat budget according to physical processes
 - analysis of sea level patterns
 - analysis of high/low-frequency variability
 - mechanistic understanding of physical processes (eddy-induced mixing, heat uptake, ...)

Some Published background

- Science of ocean models
 - Griffies and Treguier (2013): chapter from the 2nd edition of **Ocean Circulation and Climate**
 - Griffies (2009): chapter in **Encyclopedia of Ocean Sciences**
 - Griffies and Adcroft (2008): chapter discussing the formulation of ocean model equations from an AGU monograph.
 - Griffies (2005): “Some ocean model fundamentals”
 - Griffies (2004): monograph on ocean climate model fundamentals
- Ocean models and ocean modelling
 - Griffies et al. (2000): review of ocean climate model development
 - Griffies et al (2009): research article on Coordinated-Ocean ice Reference Experiments (COREs)
 - Griffies et al (2010): White Paper from the OceanObs09 conference summarizing the status of ocean models

Ocean Circulation and Climate, 2nd Edition (2013)

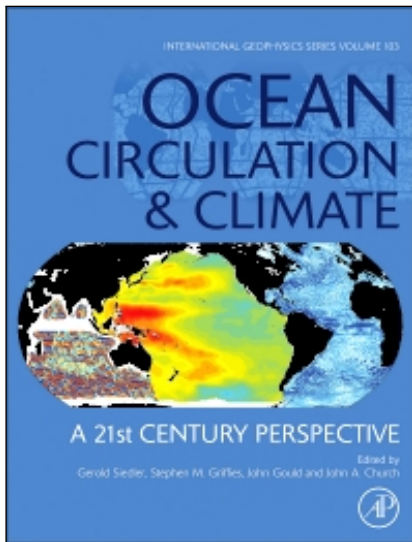


TABLE OF CONTENTS AND AUTHORS

Part I: The oceans' role in the climate system

- 1 The oceans as a component of the climate system *T. Stocker*
- 2 Paleoclimatic ocean circulation and sea level changes *S. Rahmstorf, G. Feulner*

Part II: Ocean observations

- 3 In-situ ocean observations: A brief history, present status and future directions *J. Gould, B. Sloyan, M. Visbeck*
- 4 Remote sensing of the global ocean circulation *L. Fu, R. Morrow*

Part III: Ocean processes

- 5 Exchanges through the ocean surface *S. Josey, S. Gulev, I. Yu.*
- 6 Thermodynamics of seawater *T. McDougall, R. Feistel, R. Pawlowicz*
- 7 Diapycnal mixing processes in the ocean interior *J. Markey, L. St. Laurent, A. Naveiro Garabato*
- 8 Lateral transport in the ocean interior *B. Fox-Kemper, R. Lumpkin*
- 9 Global distribution and formation of mode waters *P. Spahr, G. Ferrari*
- 10 Deep water formation *J. Bullister, M. Rhein, C. Mauritzen*

Part IV: Ocean circulation and water masses

- 11 Conceptual models of the wind-driven and thermohaline circulation *S. Drijfhout, D. Marshall, H. Nakamura*
- 12 Ocean surface circulation *A. Mouchel, L. Chassignet, R. Lumpkin*
- 13 Western boundary currents *S. Masunaga, I. Beal, B. Qiu, A. Bower*
- 14 Currents and processes along the eastern boundaries *T. Strub, O. Pizarro, V. Combes, F. Schilling*
- 15 The tropical ocean circulation and dynamics *S. Behrens, P. Brandt, G. Reverdin*
- 16 The marine cryosphere *D. Stouffer*
- 17 The Arctic and Subarctic oceans/seas *C. Mauritzen, B. Rudels, J. Toole*
- 18 Dynamics of the Southern Ocean circulation *S. Rintoul, A. Naveiro Garabato*
- 19 Inter-ocean and inter-basin exchanges *J. Sprintall, G. Stedler, H. Mercier*

Part V: Modelling the ocean climate system

- 20 Ocean circulation models and modeling *S. M. Griffies, A. M. Treguer*
- 21 Dynamically and kinematically consistent global ocean circulation and ice state estimates *C. Wunsch, P. Heimbach*
- 22 Methods and applications of ocean synthesis in climate research *A. Schiller, T. Lee, S. Masuda*
- 23 Coupled models and climate projections *P. Gani*
- 24 The oceans' role in modeling and predicting seasonal to inter-annual climate variations *B. Kirtman, T. Stocker*
- 25 The oceans' role in modeling and predicting decadal climate variations *M. Latif*
- 26 Modeling ocean biogeochemical processes and resulting tracer distributions *C. Heine, M. Gehlin*

Part VI: The changing ocean

- 27 Sea level and ocean heat content change *J. Church, N. White, C. Domingues, D. Moussallem*
- 28 Long-term salinity changes and implications for the global water cycle *P. Durack, S. Wijffels*
- 29 Ocean heat transport *A. Macdonald, M. Baringer*
- 30 The marine carbon cycle and ocean carbon inventories *T. Tanhua, N. Bates, A. Körtzinger*
- 31 Marine ecosystems, biogeochemistry, and climate *S. Doney*

General motivational comments

- Ocean model fundamentals and the use of ocean models as a tool for science involves some of the most difficult problems in classical and computational physics.
 - turbulence closures and subgrid scale parameterizations
 - analysis and rationalization of massive datasets
 - efficient methods for discretizing continuous media.
- We are also touching on elements of the most important environmental and societal problem facing the planet.
 - Climate warming is happening and humans are the key reason.
 - The ocean's role in the earth climate is significant.
 - Providing rational and robust models for understanding and predicting climate is a central element of oceanography and climate science.
 - Now is an incredibly exciting time to enter this field, particularly for those who feel passionate about diving deep into some of the most difficult intellectual problems in science while addressing some of the most important problems for the biosphere.

Outline

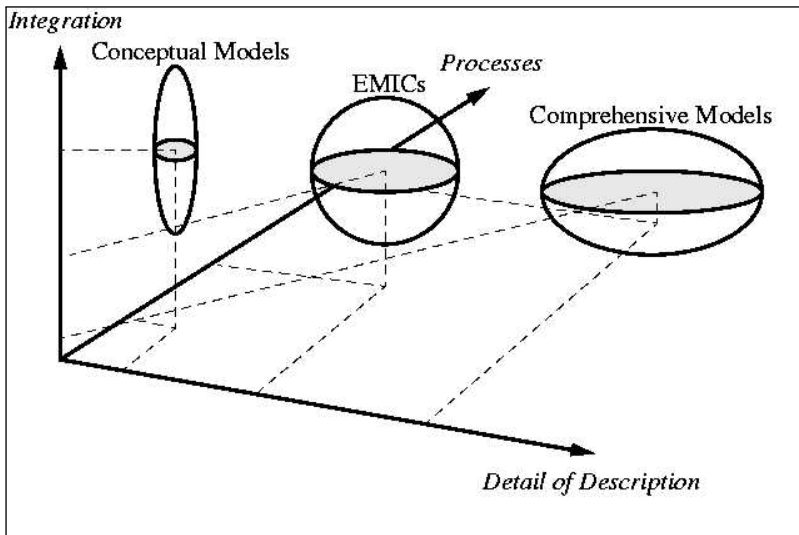
2 Motivation for using ocean models

Why use ocean models?

Ocean models are ubiquitous in ocean/climate science. Why?

- Numerical models are the primary means available for probing, in a nearly controlled manner, the ocean/climate system.
 - There is one natural ocean, yet many numerical oceans.
- Model foundations have improved through better understanding of the ocean (theory, observations, laboratory) and enhanced numerical methods.
- Computer power has increased to allow for refined resolution incorporating more details resulting in improved realism.

Types of ocean and climate models



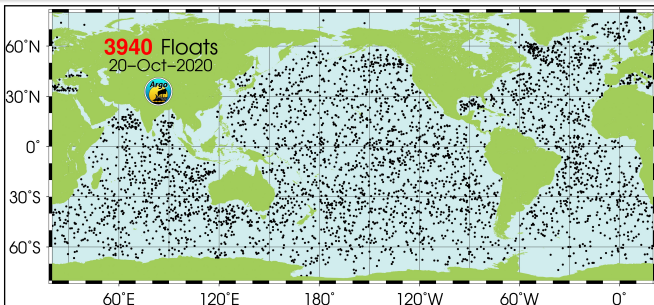
Some specific applications

- Mechanistic studies of ocean and climate processes
 - Process studies using fine resolution (≤ 1 km) simulations ([MITgcm](#), [SUNTANS](#))
 - Mechanisms for coastal and shelf processes (≤ 10 km) ([ROMS](#))
 - Mechanisms for observed large-scale variations (≤ 200 km) ([CLIVAR CORE](#))
 - Mechanisms for climate variability (≤ 200 km) ([MOM](#), [NEMO](#), [ICCM](#))
- Operational predictions and state estimation
 - Coastal forecasting ([BLUElink](#))
 - Ocean state estimation ([ECCO](#))
- Projections for future climate change
 - IPCC-class simulations with anthropogenic forcing ([CMIP](#))
 - Sea level changes ([John Church's research group](#))
 - Changes in sea ice ([NOAA info page](#))

Revolution in ocean obs requires models to interpret

Near-global observations are pushing models to improve.

Argo + satellites provide high quality near-global information relevant for predictions and climate change.



From [Argo at UCSD](#)

Outline

3 Posing the ocean model problem

Daily SST animation from GFDL CM2.6 climate model

This coupled climate model uses a 0.1° configuration of MOM5 for the ocean component, under a 50 km global atmosphere.

Theoretical foundations for ocean models

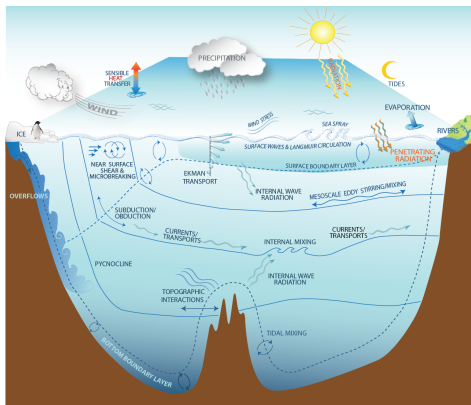
- Continuum thermo-hydrodynamical equations of the ocean
 - Seawater mass conservation
 - Tracer mass conservation
 - Momentum conservation
 - Linear irreversible thermodynamics of seawater
 - Typically assume hydrostatic balance
- Boundary conditions
 - Air-sea interactions
 - Sea ice-ocean interactions
 - Ice shelf-ocean interactions
 - Solid-earth-ocean interactions
- Subgrid scale parameterizations
 - Momentum closure: frictional stress tensor
 - Tracer closure: transport tensor
 - Boundary layer parameterizations

A sample of ocean processes

Slides in this section

- A zoo of physical ocean processes
- Space-time diagram of ocean motions
- Upper ocean boundary and wave interactions
- The marginal ice zone (MIZ)
- Southern Ocean processes
- The value of idealized Southern Ocean simulations

A zoo of physical ocean processes

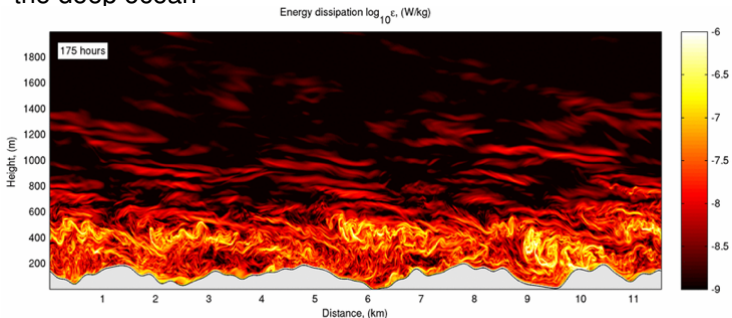


- The ocean contains a zoo of physical processes!
- Strong coupling between processes \Leftrightarrow no spectral gap.
- Coupling means it is generally better to resolve than parameterize.
- Yet we cannot resolve everything.

From Griffies and Treguer (2013)

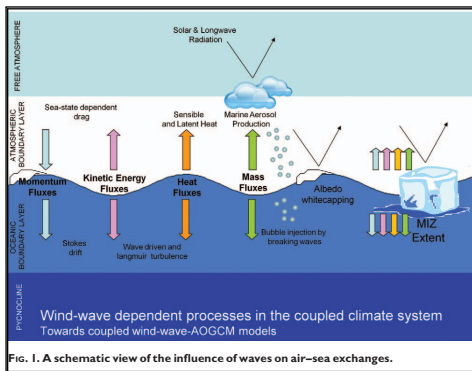
topographic Interactions

- Topographic wave generation is a significant sink of energy for geostrophic flows and a source of energy for turbulent mixing in the deep ocean



- About 1/3 comes from geostrophic motions flowing over rough topography in the Southern Ocean.
- Lee wave-driven mixing should be represented in ocean and climate models, but currently it is not!

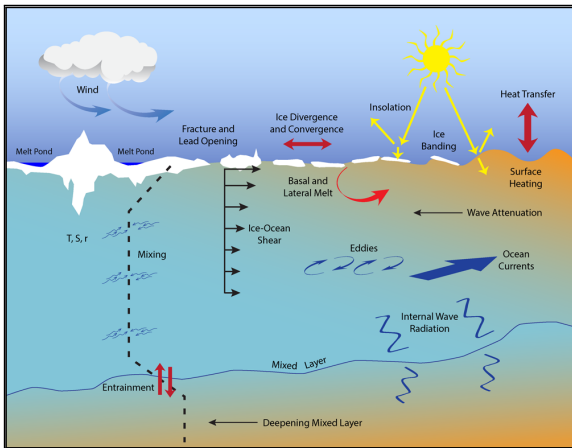
Upper ocean boundary and wave interactions



From Cavalieri et al (2012)

- New research activities in boundary layer param prompted by refined atmos and ocean resolutions that admit new dynamical regimes (e.g., mesoscale eddies, tropical cyclones).
- An increased awareness in the climate community of the importance of surface ocean gravity waves (e.g., Cavalieri et al (2012)).

The marginal ice zone (MIZ)



Questions about processes at the marginal ice zone are of prime importance as Arctic sea ice melts.

Southern Ocean processes

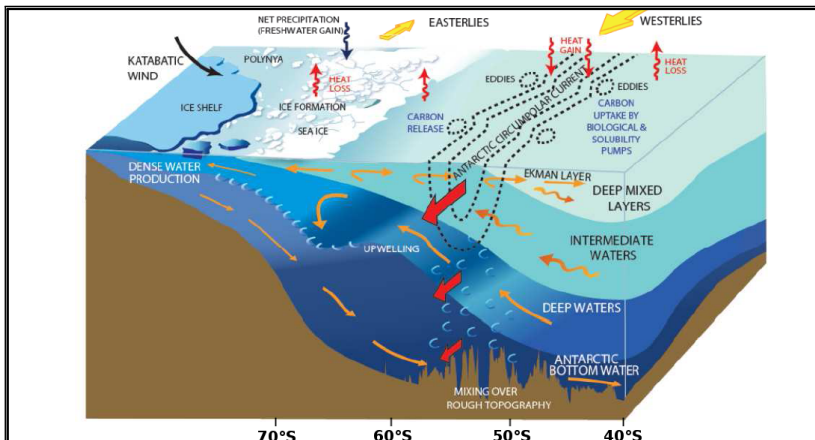
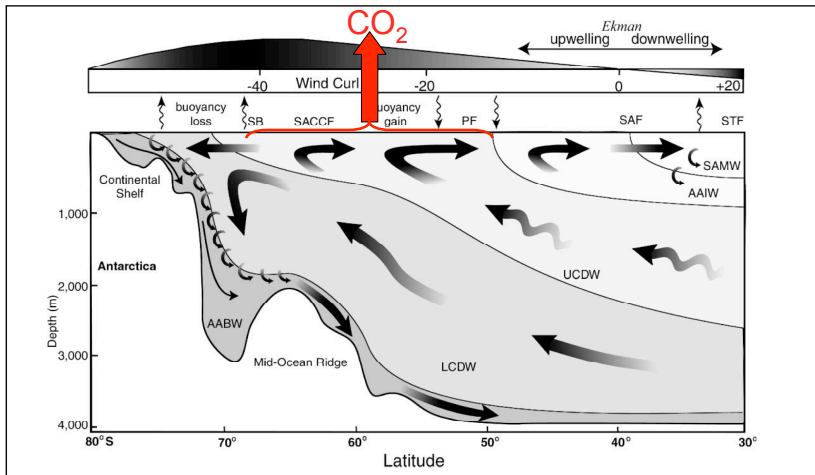
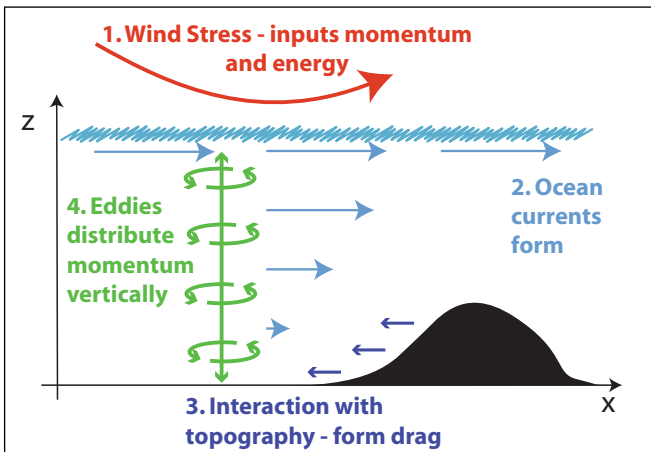


Fig. 1: Schematic of the Southern Ocean circulation, showing the numerous relevant physical and biogeochemical processes [courtesy of L. Talley].

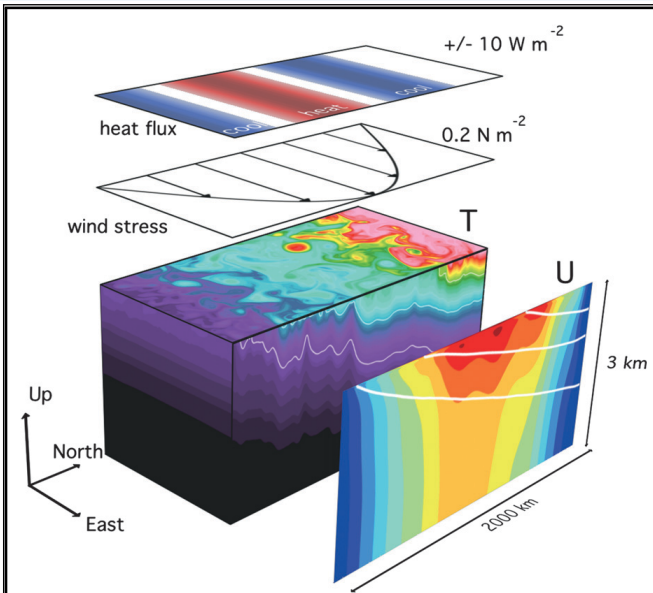
Southern Ocean processes



Southern Ocean processes



A Southern Ocean process study

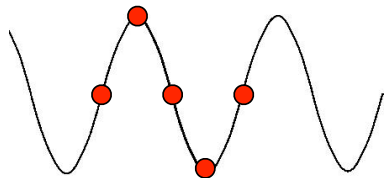


Resolving versus parameterizing: some numbers

- Direct Numerical Simulation (DNS) of global ocean climate requires 3×10^{10} time steps of one second (1000 years).
- Setting the model's grid scale to the Kolmogorov length $\Delta = 10^{-3}\text{m}$ over a global ocean domain of volume $1.3 \times 10^{18}\text{ m}^3$ requires 1.3×10^{27} discrete grid cells. This is roughly $10^4 \times$ Avogadro's number!
- Each model grid point has a velocity vector and tracer fields to time integrate.
- Conclude:
 - We will be dust long before DNS of global ocean climate.
 - We must use parameterizations to simulate the ocean.
 - The rationalization of a DNS simulation typically requires a coarse-grained perspective, as certainly would DNS of the World Ocean climate.

Facets of what we mean by “resolution”

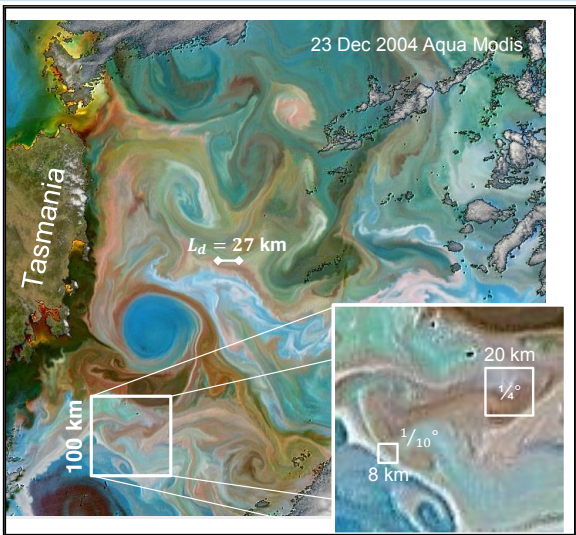
- general principles of resolution are the same for both atmospheric and ocean models
- there are different rules of thumb: one is that it takes 5 grid points to accurately define a feature without aliasing
- this means **1/8°** global resolution with an average horizontal grid cell of **14 km** can accurately depict only features larger than **56 km**
- models with variable grid spacing have variable resolution - beware of resolution-dependent physics!
- resolution is not cheap - because of the CFL* condition, as we shrink the horizontal grid spacing we must add vertical layers and decrease the time step



“every halving of the grid spacing requires roughly ten times as many computations”

* no transport faster than one grid cell per time step!

Spatial scale of mesoscale and submesoscale eddies



MODIS satellite w/ inserts by A. Adcroft (GFDL)

How to bridge the gap? Hierarchical Modelling!

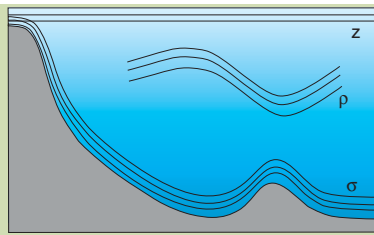


Outline

4 The vertical

Vertical coordinate representation

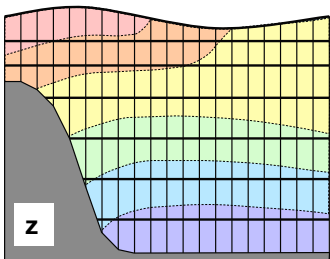
Schematic of an ocean basin illustrating the three regimes of the ocean general circulation to the considerations of an appropriate vertical coordinate. The surface mixed layer is naturally represented using fixed-depth z (or pressure p) coordinates, the interior is naturally represented using isopycnal ρ (density tracking) coordinates; and the bottom boundary is naturally represented using terrain-following σ coordinates (after Griffies et al., 2000).



Adapted by Chassignet et al (2006) from original figure in Griffies et al (2000)

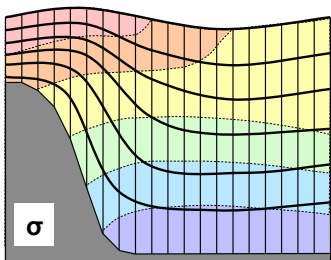
- GEOPOTENTIAL OR PRESSURE: common for non-hydrostatic process modelling and large-scale climate modelling ([MITgcm](#), [MOM](#), [NEMO](#))
- ISOPYCNAL: clean representation of interior quasi-adiabatic flows and overflows ([GOLD](#), [HYCOM](#))
- SIGMA OR TERRAIN FOLLOWING: common for shelf/coastal modelling ([ROMS](#))

Geopotential or pressure vertical coordinates



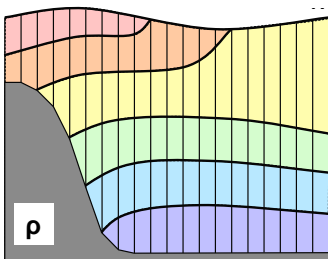
- Most common method for global models; extensive experience.
- Generalizations: $z^* = H(z - \eta)/(H + \eta)$ absorbs SSH undulations; pressure (mass conserving).
- Spurious diapycnal mixing if poorly chosen numerical methods & parameter settings (e.g., Ilicak et al 2012).
- Downslope flows poorly represented absent very fine resolution (Winton et al. 1998).

Sigma or terrain following vertical coordinates



- Extensive applications for coasts & shelves.
- Traditionally $\sigma = (z - \eta)/(H + \eta)$, but with generalizations.
- As for geopotential, \exists spurious diapycnal mixing with poorly chosen numerical methods & parameter settings.
- Much care is needed to handle horizontal pressure gradient calculation; generally need to smooth topography.
- There are very few global climate realizations.

Isopycnal vertical coordinates



- Quasi-adiabatic interior & flow-topography interactions (e.g., overflows)
- Inherently poor representation if weak vertical stratification (e.g., Labrador Sea, Southern Ocean, coastal regions).
- Care needed to represent realistic ocean thermodynamics and conservative transport, though proven methods now common.
- GFDL-GOLD, HYCOM, and Bergen: respectable climate efforts.

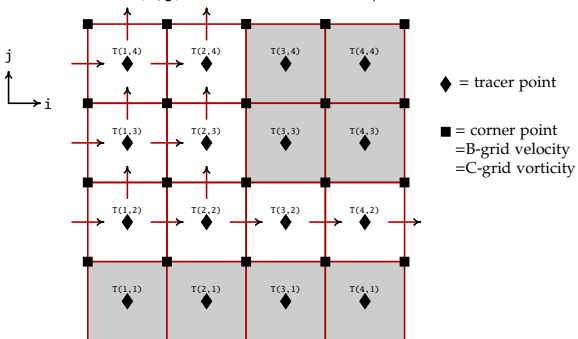
Outline

5 The horizontal



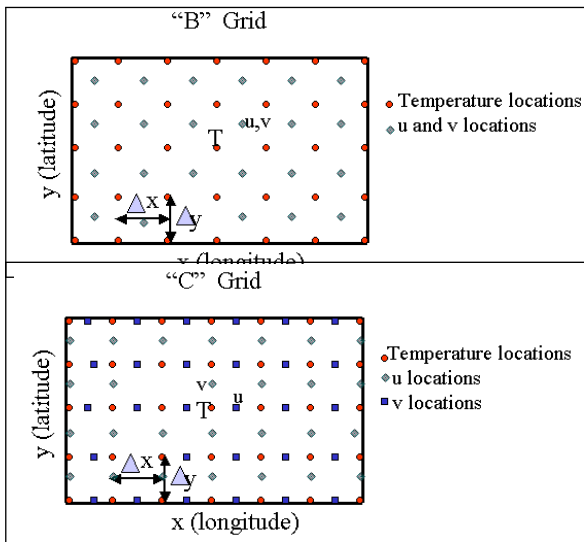
Horizontal representation: structured finite volume

TRACER CELLS $T(i, j)$ WITH FLUXES AND LAND/SEA MASKING

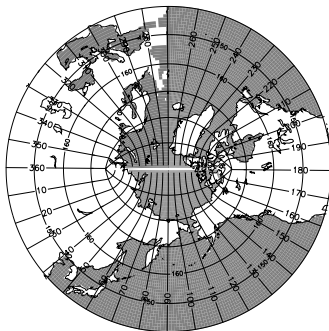


- Most common approach since 1960s; e.g., [HYCOM](#), [MITgcm](#), [MOM](#), [NEMO](#), [ROMS](#).
- Recent advances with nesting allow for multi-scale simulations (Debreu and Blayo, 2008)

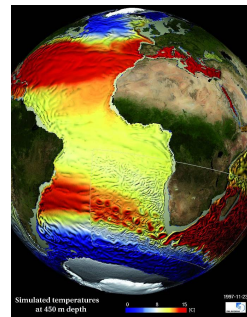
Horizontal representation: structured finite volume



Examples of structured finite volume grids



From Griffies et al (2005)



From Biastoch et al (2009)

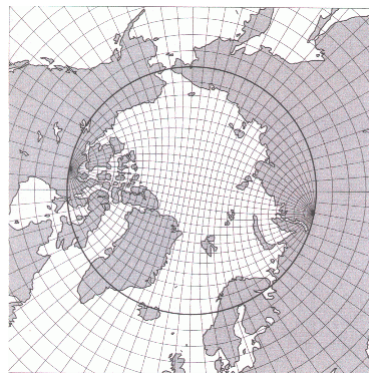
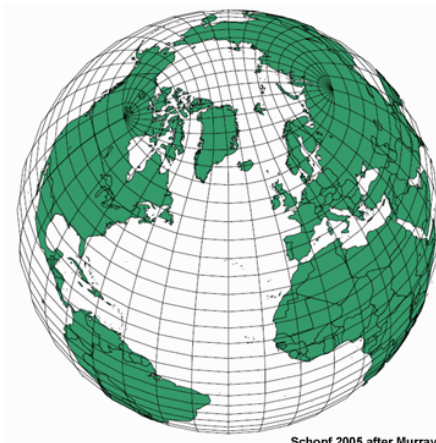
- Tripolar common for global models
- Nested example has refined grid (0.1°) around South Africa embedded in global grid (0.5°) to examine Agulhas eddies impact on Atlantic circulation.

Tripolar grids

- Regular latitude-longitude grids have a problem when they approach the poles: grid lines tend to converge, resulting in shrinking grid cells. And at some point, grid lines converge on a single point, which is difficult for models to handle computationally. One way ocean models deal with this problem is to lay a circular grid over the arctic polar region, thus eliminating a north pole. While this circular arctic grid has two points of grid convergence rather than one, they can be positioned over land. We refer to the resulting model grid as a tripolar grid.

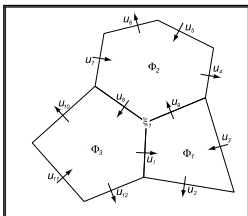
Tripolar grids

Tripolar Grid



Schopf 2005 after Murray 1996

Horizontal representation: unstructured finite volume

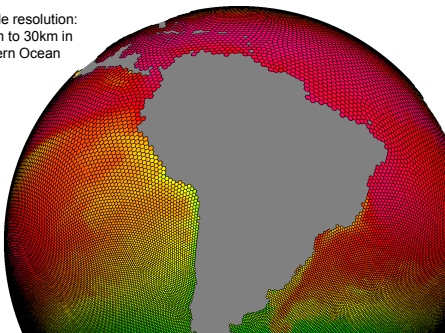


- Aimed at seamless representation of multiple-scales.
- Can obtain enhanced conservation properties in discrete equations.
- Indirect addressing of algorithms adds computational cost (i.e., number of neighbors unknown *a priori*).
- Los Alamos and NCAR have a maturing effort: [MPAS-ocean](#) (Ringler et al 2013).
- Nascent effort ongoing at [MPI-ICON](#)

Example of unstructured finite volume grid

MPAS Horizontally Unstructured Grids

Variable resolution:
120 km to 30km in
Southern Ocean



Compliments of M. Petersen, LANL (2013)

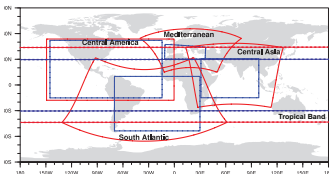
- Refined resolution towards Southern Ocean.
- Note: this is not from a working model; it is a mere example of the grid capabilities.

Regional Modelling

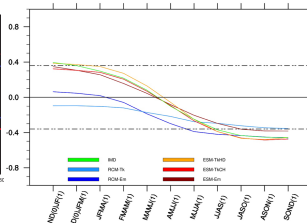
Regional Ocean Modeling: a Regional Earth System Coupled Model

- We developed a regional coupled model (ocean-atmosphere-land-hydrology-bgc)
- air-sea feedbacks largely improve the representation of intraseasonal and interannual modes of variability of the Indian Summer Monsoon Rainfall (ISMR)

Some of the initial domains where the regional Coupled model was tested



Correlation between Nino3.4 and ISMR is closer to observations in RegCM-ES

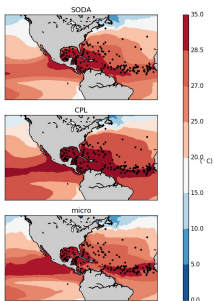


Sitz et al., 2017; Barreiro et al., 2018; Di Sante et al., 2019; Reale et al., 2019

Regional Modelling

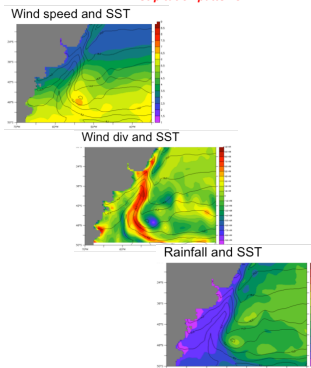
Regional Ocean Modeling: a Regional Earth System Coupled Model

*The ability to reproduce the Atlantic Warm Pool
And Tropical Cyclone cyclogenesis*



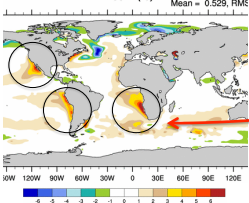
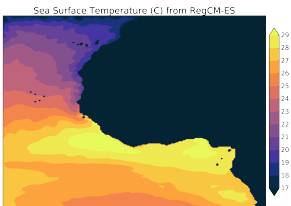
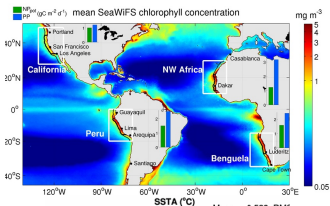
(Work carried out by a Diploma student)

*Effects of air-sea coupling of regional-scale
Precipitation patterns*



Regional Modelling

Eastern Boundary Upwelling Systems (EBUS)



- The largest biases in Temperature are found in large Upwelling systems, where small-scale processes are not represented explicitly in climate models

Outline

6 Where we are

Frontier issues I

1 Role of mesoscale eddies in climate

- Global models are increasingly being run with an explicit representation (albeit imperfect) of the mesoscales.
- How/will climate sensitivity, variability, predictability be modified with eddying ocean simulations?
- How well do our parameterized models reflect the eddying simulations?

2 Parameterizations, including stochastic methods

- Although many modelling centres can now run eddying simulations, we will need mesoscale eddy parameterizations for many decades.
- Stochastic methods are being successfully used for atmospheric parameterizations, and they are taking root for ocean parameterizations as well.

Frontiers issues II

1 Multi-scale modelling

- Whether structured (with nesting) or unstructured, models are being applied to address problems with multiple scales.
- Impacts of coast on large-scale, and converse.
- Seamless modelling is a dream that is being pushed for scientific and non-scientific reasons.

2 Coupling circulation models to surface wave models

- As ocean and atmospheric models refine resolution, traditional methods for parameterizing air-sea interface start to break down; e.g., Monin-Obukov similarity theory shows its limitations.
- The upper ocean exhibits waves, and waves affect the coupling.
- Ocean surface waves affect air-sea interactions as well as upper ocean mixing.

Trust but verify

Models are most useful when appreciating their limitations.

- Model limitations arise from:
 - fundamentals and/or numerical methods;
 - configuration design;
 - boundary information and/or other component models;
 - computational power.
- Do not treat models as a black box.
 - Models are tools to help deduce mechanisms.
 - Use diagnostic methods to uncover reasons for particular behaviour.
- Numerical errors often appear in physically interesting manners.
 - Remain skeptical even if the simulation “looks right”.
 - Investigate why and how.
 - The more one learns about models, the more one can sense whether a particular simulation is physically sensible or the artefact of faulty methods.

Wherein lies the truth?

Perspectives on models

- Models cannot be *validated*. At best, they can be *evaluated* (see Oreskes et al 1994).
- “All models are wrong, but some are useful.” (G.E.P. Box, statistician)

Outline

7 References and further reading

References and recommended tutorials I

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